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All-fiber nonlinearity- and dispersion-managed dissipative soliton nanotube mode-locked laser

Z. Zhang,^{1,2} D. Popa,^{3,a)} V. J. Wittwer,³ S. Milana,³ T. Hasan,³ Z. Jiang,³ A. C. Ferrari,³ and F. O. Ilday^{1,4}

¹*Department of Physics, Bilkent University, 06800 Ankara, Turkey*

²*Nanjing University of Posts and Communications, Nanjing 210003, China*

³*Cambridge Graphene Centre, University of Cambridge, Cambridge CB3 0FA, United Kingdom*

⁴*Department of Electrical and Electronics Engineering, Bilkent University, 06800 Ankara, Turkey*

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We report dissipative soliton generation from an Yb-doped all-fiber nonlinearity- and dispersion-managed nanotube mode-locked laser. A simple all-fiber ring cavity exploits a photonic crystal fiber for both nonlinearity enhancement and dispersion compensation. The laser generates stable dissipative solitons with large linear chirp in the net normal dispersion regime. Pulses that are 8.7 ps long are externally compressed to 118 fs, outperforming current nanotube-based Yb-doped fiber laser designs. © 2015 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4937461>]

Passively mode-locked fiber lasers are established tools for generating ultrafast pulses due to their compact design,^{1,2} misalignment-free waveguide format,^{1,2} and low cost,^{1,2} while providing a convenient platform for the study of new mode-locking regimes.^{3–5} Mode-locked pulse characteristics are determined by the interaction of dispersion and nonlinear effects.^{4–6} A common approach relies on soliton mode-locking,⁷ where anomalous (negative) dispersion effects are balanced by intensity-dependent nonlinear effects triggered by the pulse itself.⁸ As the net cavity dispersion approaches zero, the laser generates dispersion-managed solitons⁸ or stretched pulses,⁹ with higher pulse energy ranging from hundreds of pJ (Refs. 8 and 9) up to few nJ,^{10,11} than in a soliton laser, where the typical output is in the tens of pJ per pulse range.^{8,9} Cavities with positive (normal) dispersion, such as similariton^{3,4} or all-normal dispersion lasers,¹² can produce highly chirped pulses with energies up to tens of hundreds of nJ.^{12,13} These pulses are termed dissipative solitons (DS),^{5,6} with the pulse shaping mechanism based, in part, on spectral filtering of the chirped pulse, which trims the temporal wings of the pulse.¹² There is great interest in developing DS lasers,⁶ as they can emit stable, high-energy pulses¹² that can be compressed to transform-limited pulses with numerous applications.¹⁴ All-fiber cavity designs are preferred for their environmental robustness. A route to enable stable, 100 fs range, DS is to combine both dispersion and nonlinearity management,¹⁶ especially for lasers operating at $\sim 1\ \mu\text{m}$ where standard fiber has normal dispersion only.¹⁴ In order to provide sufficient dispersion and nonlinear effects, few-kilometer-long cavities have been used,¹⁷ achieving stable, linearly polarized nanosecond pulses.¹⁸ However, despite their long, $\sim\text{ns}$ range, pulses, such long cavities have repetition rates of hundreds of kHz (e.g., 1 km corresponds to $\sim 200\ \text{kHz}$),^{17,18} often not desirable in applications such as nano-surgery¹⁹ or two-photon microscopy,²⁰ where there is a trade-off between the repetition rate and the multi-photon signal generated.²⁰

While nonlinear effects are essential for mode-locking,^{3,4} excessive nonlinearity can result in noise-like or multiple pulse operation.³ Nonlinearity management has been proposed as a way of preventing spectral sideband formation in soliton fiber lasers,¹⁶ with consequently higher pulse energy,¹⁶ while it can be beneficially exploited towards, e.g., similariton generation,^{3,4} spectral broadening, and supercontinuum generation in nonlinear optical fibers.²¹ Similarly, a lack of nonlinearities can also compromise mode-locking formation. For example, management towards increasing nonlinearities was proposed by using quasi-phase-matching devices in free-space solid-state lasers.²² Thus, nonlinearity management is an important aspect of laser design, in order to design stable, 100 fs range, mode-locking.^{16,22} Photonic crystal fibers (PCFs),²³ i.e., silica fibers with an ordered array of air-holes along their length,²³ enable advanced dispersion and nonlinearity control in fiber format,²³ primarily determined by the air-hole spacing,²³ thus offering possibilities for both nonlinearity and dispersion management in fiber lasers.^{24,25}

Carbon nanotubes (CNTs) and graphene have emerged as promising saturable absorbers (SAs)^{26–28} with ultrafast recovery time,^{29,30} able to support short pulses,^{31,32} and with a number of favorable properties for laser development, such as broadband operation,^{33,34} and ease of fabrication²⁷ and integration²⁷ into all-fiber configurations.^{35–38} Broadband operation is an intrinsic property of graphene,³⁹ while in CNTs this can be achieved using a distribution of tube diameters.³³ A variety of techniques have been implemented in order to integrate CNTs and graphene into lasers.^{40–42} For example, graphene can be integrated into various optical components, with the possibility of controlling the modulation depth.⁴³ CNTs and graphene can also be embedded in polymer matrices that can be integrated into fiber lasers.^{26,27} CNT composites can exhibit high ($\sim 20\%$ (Ref. 32)) modulation depths,^{32,33} preferred for mode-locking of fiber lasers, that typically operate with higher gain and cavity losses² than their solid-state counterparts.⁴⁴ Although CNT mode-locked DSs have been reported at $\sim 1.5\ \mu\text{m}$ by exploiting dispersion management,¹⁵ nonlinearity management is also

^{a)}Electronic mail: dp387@cam.ac.uk

required¹⁶ in order to generate stable, ~ 100 fs range DS, even more important for all-fiber lasers operating at ~ 1 μm , where the normal dispersion of silica is dominant.¹⁴

Here, we demonstrate a DS, all-fiber Yb-doped (YDF) laser based on a CNT-SA, operating at ~ 1040 nm. To retain the all-fiber format, a length of PCF is used for nonlinearity and dispersion management. As a result, DSs are generated in a compact 34-MHz repetition rate laser. Highly chirped, 8.7-ps pulses, are externally compressed in a second-order, β_2 , grating pair dispersive delay line, close to their transform-limited duration of 118 fs, the shortest to date for CNT YDF DSs fiber lasers. We perform numerical simulations to confirm DS operation.

For our fiber laser design, we use a CNT-SA. To match the operation wavelength of the YDF laser (~ 1040 nm,⁴⁵ i.e., ~ 1.19 eV), CNTs with ~ 0.8 nm diameter are required, since this diameter corresponds to a band-gap ~ 1.18 eV.⁴⁶ We use CNTs produced by catalytic disproportionation of CO (CoMoCAT),^{47,48} with a 0.6–1.2 nm diameter distribution.⁴⁸ In order to monitor defects before and after composite fabrication, we measure the Raman spectra of the CoMoCAT powders (red curves) at 633 nm, using a Renishaw InVia micro-Raman spectrometer equipped with a 100X objective (N.A. = 0.85). The power is kept below 500 μW to avoid damage and laser-induced heating. Fig. 1(a) plots the Raman spectra of the CNT powder in the G region. The relative intensity of the D to G peaks, $I(\text{D})/I(\text{G})$, can be used to quantify defects.^{49–51} A polymer composite is then fabricated via solution processing, using polyvinyl alcohol (PVA).²⁷ The Raman spectra of the CNT-PVA film, Fig. 1(a) (black curve) does not show any increase in $I(\text{D})/I(\text{G})$, indicating that the fabrication process does not induce significant structural damage. Fig. 1(b) plots the absorbance of the PVA (blue line) and the CNT-PVA composite (black line). The latter has a peak between 980 and 1100 nm, which covers the desired operating wavelength, 1040 nm. The absorbance of the PVA is ~ 1 order of magnitude lower than that of the CNT-PVA composite, in the 400–1600 nm range, thus negligible.

For our all-fiber laser, we implement a ring cavity, as shown in Fig. 2(a). The net dispersion is kept normal to support DS.^{5,6} The gain section is a 1.88 m YDF with $\beta_2 = 35.5$ fs^2/mm , followed by a 20% output coupler and an inline isolator. We use a 2.1 m solid-core PCF for nonlinearity and dispersion management, with an air-hole diameter of 1.2 μm and an air-hole spacing of 2.0 μm , characterised using a scanning electron microscope (SEM) (Fig. 2(b)), corresponding to a nonlinear coefficient of $52 \text{ W}^{-1}\text{km}^{-1}$ and $\beta_2 = -46.3$ fs^2/mm .²⁵

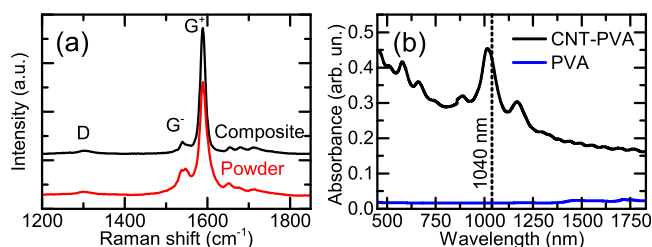


FIG. 1. (a) Raman spectra at 633 nm for (red lines) powders and (black lines) CNT-PVA in the G peak region. (b) Absorbance of CNT-PVA (black line) and PVA (blue line). Our mode-locked laser operating wavelength is marked by the dotted line.

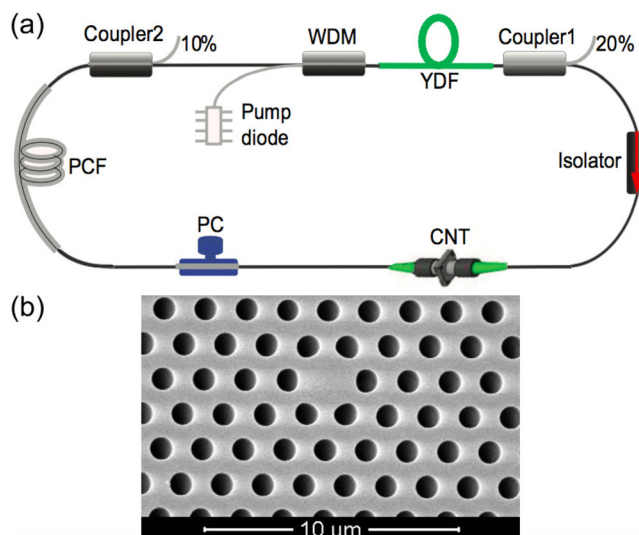


FIG. 2. (a) Schematic of the all-fiber dissipative soliton Yb-doped fiber laser using a CNT-SA and a PCF for nonlinearity and dispersion management. (b) SEM image of the PCF.

All other fibers used in the cavity are standard single-mode fibers (SMF-28 from Corning). The intracavity dispersion is estimated to be ~ 0.014 ps^2 , comparable to that typically reported for DS lasers.^{5,6} The CNT-SA is then integrated into the cavity between a pair of fiber connectors.²⁷ For intracavity polarization adjustment (mode-locking optimization) a polarization controller (PC) is placed after the CNT-SA. Another 10:90 coupler is used to monitor the output before the wavelength-division multiplexer (WDM). The cavity length is ~ 6 m, corresponding to a repetition rate of 34 MHz.

Characterization of mode-locked operation is presented in Fig. 3. Onset of continuous-wave (CW) and mode-locked operations are observed at pump powers (P_p) of 51 mW and 74 mW, respectively. A set of mode-locked output spectra is recorded for a constant $P_p = 92$ mW, and presented in Figs. 3(a) and 3(b) on a logarithmic and linear scale, respectively. The spectrum exhibits steep edges, as a result of spectral filtering,¹² typical signature of DS,⁶ with 17.6 nm spectral

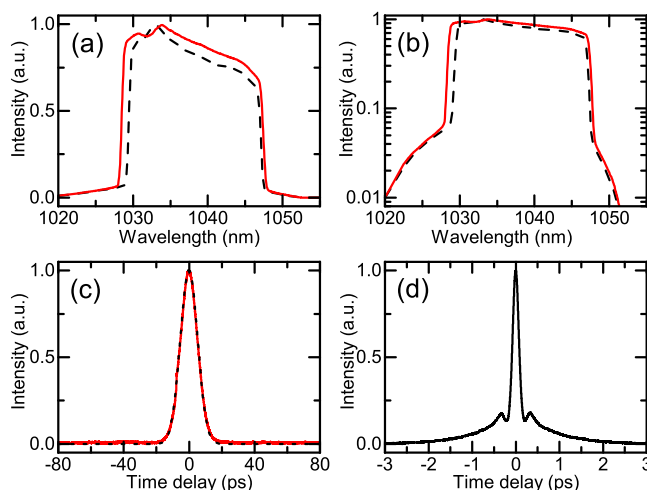


FIG. 3. Optical spectra measured from couplers before (black, dashed line) and after (red, solid line) YDF on (a) linear and (b) logarithmic scale. (c) Autocorrelation trace of the chirped pulse (red, solid line) and its Gaussian fit (black, dashed line). (d) Autocorrelation trace of the dechirped pulse.

width. The corresponding autocorrelation trace of the chirped pulse is presented in Fig. 3(c). Assuming a Gaussian profile, this gives a pulse duration of 8.7 ps. The time-bandwidth product (TBP) is ~ 100 times the expected transform-limit value of 0.44.⁸ Using a grating pair, with anomalous dispersion -0.25 ps^2 , seed pulses are de-chirped to 118 fs (Fig. 3(d)). The resulting TBP is ~ 0.57 , close to the transform-limit, indicating that the chirp is predominantly linear. After de-chirping, an increased pedestal is observed, likely due to uncompensated dispersion and nonlinearities associated with the pulse propagation in the PCF.²⁵

In order to better understand the mode-locking dynamics, we perform numerical simulations based on a modified nonlinear Schrödinger equation model, described in Ref. 4. The evolution of the temporal and spectral widths along the cavity is shown in Fig. 4(a). The pulse duration and spectral width increase monotonously in the YDF and the following SMF segments, which have normal dispersion. As expected, the pulse duration decreases in the PCF segment due to its anomalous dispersion, and increases back slightly in the following SMF segment. The spectral width also increases in the PCF segment due to self-phase modulation. Fig. 4(b) plots the output spectra after the YDF and before the WDM. Their bandwidths are 17.3 and 17.1 nm, respectively. Fig. 4(c) shows a 7.2 ps-long pulse after the YDF. The overall evolution indicates that pulses remain highly chirped throughout the cavity, and temporal breathing is much smaller than in traditional dispersion-managed lasers.⁸ The accumulated nonlinear phase shift in the PCF is estimated to be 0.86π . This should be contrasted to the case of no dispersion or nonlinearity management, as would be obtained by replacing the PCF with regular SMF of equal length: the resulting nonlinear phase shift is 0.13π , which is 7 times smaller. However, in such configuration mode-locking could never be initiated.

We then consider the effect of dispersion on the DS operation. We change the SMF length to vary the dispersion. We achieve stable operation with steep-edge spectral shape within a $0.11\text{-}0.026 \text{ ps}^2$ dispersion range. The laser exhibits

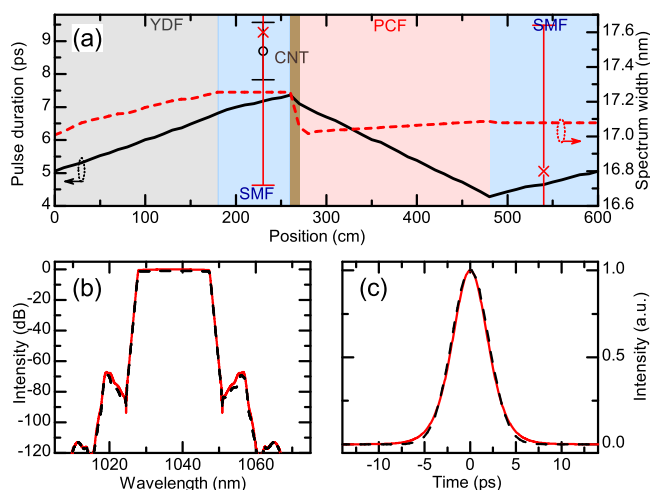


FIG. 4. Simulations. (a) Evolution of the temporal and spectral widths as a function of position along the cavity. (b) Spectra after the YDF (red, solid line) and before the WDM (black, dashed line). (c) Pulse shape after the YDF (red, solid line) and its Gaussian fit (black, dashed line).

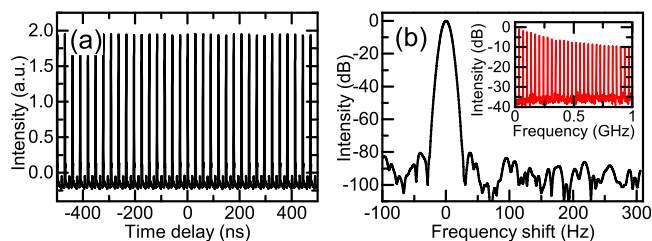


FIG. 5. (a) Output pulse train. (b) RF spectrum with 500 Hz span and 1 Hz resolution with central frequency shifted to zero for clarity, inset shows the RF harmonics over a scan range of 1 GHz, with 500 kHz resolution bandwidth.

Q-switching with no spectral steep-edge signature outside this range, showcasing the importance of dispersion management for stable DS formation. The spectral width broadens with pump power. The maximum output power is $\sim 3.5 \text{ mW}$, for a pump power of $\sim 100 \text{ mW}$, corresponding to an intracavity pulse energy of 0.5 nJ . Even broader spectral width, combined with shorter pulse duration and higher output power, may be achieved by further improvement of the cavity design. For example, by employing evanescent-field interaction, the CNT-SA would be exposed to only a fraction of the field, with the interaction length extended up to mm, thus avoiding high optical densities for higher-power pumping designs.

The laser stability is characterized through radio frequency (RF) measurements.⁵² Fig. 5(b) plots the RF spectrum around the fundamental cavity round-trip frequency of 34 MHz with 1-Hz resolution bandwidth and 500-Hz scanning range. An 80 dB signal-to-noise ratio is observed, indicating low amplitude fluctuations. There is no spectral modulation over 1 GHz [see inset of Fig. 5(b)], which, when combined with long-range autocorrelation measurements, rules out multiple pulsing.

In conclusion, we reported the generation of DS from an all-fiber laser. The use of a PCF, for both nonlinearity and dispersion management, results in stable, self-starting mode-locking, with large linear chirp. Nonlinearity management enables mode-locking at relatively low pump power. The output pulses can be externally compressed to 118 fs. Given the high repetition rate, short pulses generated from an environmentally robust, all-fiber cavity architecture. Our results might be used in a variety of applications, such as nonlinear imaging, nano-surgery, or spectroscopy.

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