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Ultrathin phase-change coatings on metals for electrothermally tunable colors

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Metal surfaces coated with ultrathin lossy dielectrics enable color generation through strong interferences in the visible spectrum. Using a phase-change thin film as the coating layer offers tuning the generated color by crystallization or re-amorphization. Here, we study the optical response of surfaces consisting of thin (5–40 nm) phase-changing Ge₂Sb₂Te₅ (GST) films on metal, primarily Al, layers. A color scale ranging from yellow to red to blue that is obtained using different thicknesses of as-deposited amorphous GST layers turns dim gray upon annealing-induced crystallization of the GST. Moreover, when a relatively thick (>100 nm) and lossless dielectric film is introduced between the GST and Al layers, optical cavity modes are observed, offering a rich color gamut at the expense of the angle independent optical response. Finally, a color pixel structure is proposed for ultrahigh resolution (pixel size: $5 \times 5 \ \mu m^2$), non-volatile displays, where the metal layer acting like a mirror is used as a heater element. The electrothermal simulations of such a pixel structure suggest that crystallization and re-amorphization of the GST layer using electrical pulses are possible for electrothermal color tuning. *Published by AIP Publishing*. [http://dx.doi.org/10.1063/1.4961368]

Strong absorption of light can be achieved through strong interference effects enabled by nanometers thick lossy dielectrics on reflective layers such as metals. Recently, such surfaces have been investigated for color generation/printing,^{1–4} enhanced light absorption in the visible⁵ through Ge or Si coating of metals like Au and Ag, and infrared (IR) filters⁶ and emitters⁷ using thin VO_2 on sapphire. Moreover, phase-changing Ge₂Sb₂Te₅ (GST) films on Au are demonstrated for enhanced optical data storage using the same optical phenomenon.⁸ GST shows reversible phase transitions between amorphous and crystalline states accompanied by significant changes in its optical and electrical properties. Hence, GST and other phase-change materials are commonly used for optical^{9,10} and electrical^{11,12} data storage media. Amorphous to crystalline transition is typically achieved by annealing the material below the melting temperature for at least tens of nanoseconds.¹³ The reverse transition requires melting and quenching the material which can be achieved in a much shorter time scale (\sim fs).^{8,14} External heating^{15,16} or self-heating using lasers^{17,18} or electrical pulses^{19,20} are used for annealing or melt-quenching. Recently, GST has found its way into visible²¹ and infrared plasmonic absorber surfaces using Al nano-antennas^{14,22} and Au nanopatches.^{23,24} The optical response of the plasmonic infrared (IR) absorber surfaces is tuned by annealing on a hot $plate^{22}$ or with a train of low-power femtosecond pulses¹⁴ for amorphous to crystalline transition and a single high-power femtosecond laser pulse for crystalline to amorphous

transition.¹⁴ Very recently, electro-thermally tunable pixel structures consisting of a Pt/ITO/GST/ITO stack have been demonstrated using Fabry-Perot resonances.¹⁹

Here, we study optical responses of surfaces formed by ultrathin (5-40 nm) GST coated metal mirrors, primarily Al, and investigate their potential application as tunable color pixels for large area displays. The surfaces studied here have a simple 2-layer structure consisting of continuous thin GST films on 80 nm thick Al. The optical responses of the surfaces are tuned by annealing samples on a hot plate $(T > 150 \degree C)$ as the GST film morphology changes from the as-deposited amorphous to face-centered cubic (fcc) crystalline phase.^{14,22,25} Electrothermal simulations of a small pixel made of such GST structures are also performed to assess the possibility of achieving thermally tunable large-area displays by electrical heating. In the proposed pixel structure, the mirror layer also functions as a heater in contrast to selfheating of the GST layer in the Pt/ITO/GST/ITO stack demonstrated in Ref. 19. As a result, the proposed structure allows larger (> μ m) pixels and hence enables large-area fabrication; whereas the Pt/ITO/GST/ITO stack can offer richer color gamut.

The most commonly used metals for the plasmonic applications, i.e., Au, Ag, and Al, are considered for this study (see Figure S1 in the supplementary material for the optical constants). The initial simulation results for 20 nm amorphous GST (aGST) on optically thick Au, Ag, and Al metal layers reveal reflection minimum at \sim 640 nm for Au and Ag, and \sim 400 nm for Al (Figure 1(a)). These results show that Al enables absorptions centered around the ultraviolet (UV) wavelengths for thin film thickness values which can be reliably deposited by a sputtering system. Furthermore, the surface colors achieved using Ag mirrors

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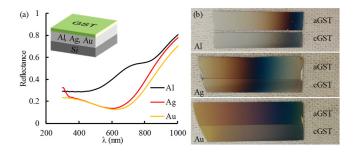


FIG. 1. GST coated metal surfaces. (a) Simulated reflection spectra of 20 nm aGST on 80 nm Al, Ag, and Au layers. (Inset) Illustration of the structures. (b) Color gradients on surfaces achieved by depositing GST films with increasing thickness from left (<5 nm) to right (>50 nm) on Al, Ag, and Au layers. Thermal color tuning is achieved only on the Al and Au bottom layers.

cannot be tuned by crystallization of the top GST layer (Figure 1(b), Figure S2 in the supplementary material). Hence, Al is preferred over Au due to its low cost and reflection minima achieved at lower wavelengths despite its interband absorption at ~800 nm.²⁶ The colors generated on the Au mirror is found to be brighter compared to what is reported by Schlich *et al.*⁸ using the Au/Ti/TiN/GST/SiO₂ stack. This is attributed to the thin (5 nm) Ti/TiN barrier layer that Schlich *et al.*⁸ used between the Au and GST layer.

The top GST thickness is varied from 5 to 140 nm to observe the reflection minimum to shift from the UV to near IR regimes (Figure S3 in the supplementary material). Colors of the surfaces can be tuned from yellow to red to blue by varying the aGST thickness from 5 to 40 nm (Figures 1(b) and 2(a)). The surfaces with as-deposited aGST films are annealed beyond 150 °C using \sim 1 K/s heating rates on a hot plate for color tuning. The surfaces look dim gray for all GST thicknesses upon crystallization (Figure 2(a)). The reflection spectra measurements reveal that the observed colors are due to absorption of certain portions of the visible regime (Figure 2(b)). The reflection spectra change upon crystallization resulting in almost constant low-reflectance in the visible regime, which is responsible for the dim gray colors. For the 20 nm GST film, the absorption wavelength to the film thickness ratio (λ/t) is 7.4 *n* for amorphous and 8 n for fcc phases of GST, both being larger than 4n which is observed for conventional interference coatings. The λ/t ratio decreases with increasing absorption wavelength, being close to 4 n, owing to decreasing extinction coefficients of aGST and crystalline GST (cGST) (Figure S1 in the supplementary material). aGST behaves like a lossless dielectric (k = 0) beyond $\lambda \sim 1.5 \,\mu m$, resulting in weak absorptions as opposed to the strong absorptions obtained in the visible regime (Figure S4 in the supplementary material). The extinction coefficient of cGST is never zero due to the Drude contribution in the near and mid-IR.²⁵ The reflection minimum in the near IR obtained using thicker (80-140 nm) aGST films consistently red-shifts and exhibits almost perfect absorptions upon crystallization because of larger *n* and non-zero *k* of cGST in this regime (Figure S4 in the supplementary material). The thermally tunable optical behavior of the surfaces in the near and mid-infrared regimes offers further photonics applications such as active spectrally selective infrared absorbers/emitters and active electric field enhancement platforms for sensitive infrared absorption spectroscopy. Simulation results using the measured complex refractive index of aGST and cGST capture the measured reflection spectra (Figure 2(c)). Figure S5 in the supplementary material shows simulation results with 5 nm GST thickness increment providing better visualization of tuning of the reflection spectra upon crystallization of the GST film.

The as-fabricated GST films are in the amorphous phase. The GST phase transitions to fcc ~ 150 °C while annealing the films on a hot plate with relatively low heating rates ($\sim 1 \text{ K/s}$). Further increment in the temperature switches the phase from fcc to hexagonal ~ 200 °C. These transition temperatures depend on the heating rate and the stress on the GST film.^{27,28} Crystallization of the top GST film while annealing can also be monitored by visually inspecting the surface color. The temperature coefficient of the refractive

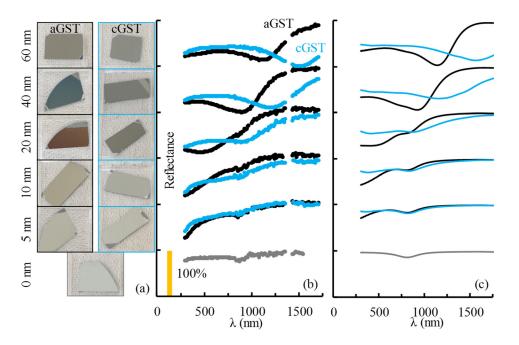


FIG. 2. Optical properties of GST coated Al surfaces. (a) Photographs of GST films with indicated thicknesses on 80 nm Al. Corresponding (b) measured (c) simulated reflection spectra. Reflection spectra scales between 0% and 100%. The curves are shifted along the y-axis. The crystallized films are expected to be 5% thinner than the as-fabricated aGST films.

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index for GST is reported to be small $(\Delta n/\Delta T = -2.5 \times 10^{-3}$ 1/K, $\Delta k/\Delta T = 6.4 \times 10^{-4}$ 1/K at 600 nm),²⁹ and hence no significant color change is observed until the amorphous to fcc-phase transition. Once the aGST films start crystallizing, the colors of the surfaces suddenly turn dim gray and stay that way as the surfaces cool down to the room temperature. Further annealing the surfaces beyond 200 °C changes the GST phase to hexagonal, which has an indistinguishable effect on the reflection spectra (Figures 3(a) and 3(b)) due to small difference in the refractive indices of GST in fcc and hexagonal-phases.²⁹

The reflection spectra and colors of the surfaces are unaffected up to high angles of incidence ($\sim 65^{\circ}$) (Figures 3(c) and 3(d)) owing to extremely thin GST layers. Similar results are observed with other strong interference surfaces such as 15 nm Ge coated Au surfaces.³ Owing to the angle-independent response of ultrathin coatings, flexible, bendable, and rough substrates such as Al foil (Figure S6 in the supplementary material) or paper⁴ can be used for the strong interference applications.

The color gamut that can be achieved with ultrathin coating of metal mirrors can be enhanced introducing a lossless film between the mirror and absorber layers (Figure 4(a)). A similar multi-layer structure, specifically a thin (7 nm) GST layer sandwiched between two ITO layers on top of a Pt mirror, has recently been used by Hosseini et al.¹⁹ for color tuning. Another recent study uses such a multilayer structure with 2 GST layers separated by a thermal barrier layer.³⁰ In the study by Hosseini et al., the bottom ITO layer thickness has been varied to adjust the color, which is also further varied by changing the GST phase using self-heating through electrical pulses. Such electrical heating requires the use of a transparent conductive material (ITO) instead of a lossless dielectric. In contrast, instead of using an ITO layer, here we use an HfO₂ layer between the top GST and bottom Al layers which enables the metal layer function as a heater as well. Optical simulation results show that a HfO₂ layer on top of Al without a GST top layer shows weak resonances in the visible regime (Figure 4(a)). A 10 nm aGST layer on top of HfO2 induces strong resonances which broaden and red-shift with increasing HfO₂ thickness (0-120 nm) and totally disappear for thicker HfO₂ (Figure

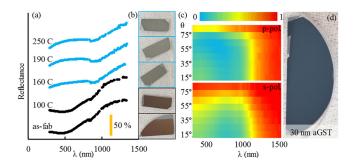


FIG. 3. The effect of annealing temperature and angle of incidence on the optical response of the surfaces. (a) Measured reflection spectra of 20 nm GST coated Al surfaces after annealing with a heating rate of ~ 1 K/s up to the temperatures shown next to each curve. The curves are shifted along the y-axis. (b) Photographs of the surfaces. (c) Measured reflection spectra of the 30 nm aGST coated Al surface as the angle of incidence is varied from 15° to 85° with 10° steps for p- and s-polarizations. (d) Photograph of the surface with 30 nm aGST.

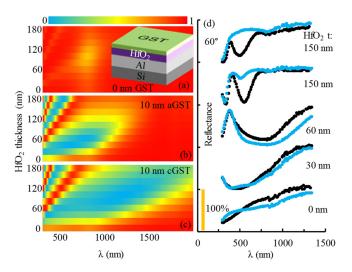


FIG. 4. The effect of the HfO_2 layer between GST and Al layers. Calculated reflection spectra for varying thickness of HfO_2 on Al (a) without GST and with (b) 10 nm aGST and (c) 10 nm cGST top layers. (Inset) Illustration of the structure. (d) Measured reflection spectra of 10 nm aGST (black) and 10 nm cGST (blue) top layers on HfO_2 films with indicated thicknesses. The curves are shifted along the y-axis. The angle of incidence for the top curves is 60° and 30° for the rest.

4(b)). Crystallization of the GST layer also broadens the resonances for thin HfO₂ (Figure 4(c)). Fabry-Pérot resonances appear for further increment in the HfO2 thickness (>80 nm).^{19,31,32} The absorption bands achieved with Fabry-Pérot resonances are narrower than those observed for strong interference effects, resulting in brighter surfaces colors. The blue-shift in the Fabry-Pérot resonances with crystallization of the top GST layer shifts the surface color to a different tone instead of a complete color change observed for the surfaces without a spacer layer. The measured reflection spectra show the broadening and red-shift of the reflection minimum and further broadening with increasing HfO₂ thickness (0-60 nm), as well as the emergence of the Fabry-Pérot resonances for 150 nm HfO₂ (Figure 4(d)). The reflection spectra and hence the colors of the surfaces with thick HfO₂ layers significantly depend on the angle of incidence as shown by the reflection measurements performed at 30° and 60° (Figure 4(d)) and the photographs taken at low and high viewing angles (Figure S7 in the supplementary material). The lossless dielectric layer between the GST and metal layers could also function as a barrier to prevent diffusion of the metal into GST, which is a great concern when chemically active metals are used in contact with GST.

The observed color gradient by changing either the GST or the dielectric thickness and color change with crystallization of the GST layer led us to study its potential for high resolution, nonvolatile, reflective displays. Both amorphous to crystalline and crystalline to amorphous phase transitions are required for a rewritable display. While simply annealing the films is enough for crystallization as presented here, amorphization requires melting and quenching the material which is typically achieved using a single femtosecond laser pulse at the film level.⁸ However, to form a display it is desired that the phase of the GST film, hence the surface color, is tuned using electrical pulses, similar to the demonstration of tiny displays (pixel size: $300 \times 300 \text{ nm}^2$) formed by the ITO/GST/ITO/Pt stack of Hosseini *et al.*¹⁹ Such dimensions, however,

do not allow large area displays as they require e-beam lithography or projection photolithography for patterning. Simply scaling up the tiny pixels formed by sandwiched GST layer for large area displays would not work, since small filaments forming in the GST layer carry most of the electrical current during amorphization pulses resulting in heating and melting of small spots in the GST layer. To uniformly heat and melt the GST layer for uniform amorphization, we propose the bottom reflector to function also as a heater (Figure 5(a)). If the electrical contacts are designed to be thicker than the metal layer ($\sim 100 \text{ nm}$), most of the electrical power is expected to be dissipated in the metal layer under the GST film. The proposed structure with 5 \times 5 μ m² area is simulated to test its heating and cooling behavior using the electrothermal (Joule heating) module of COMSOL Multiphysics. The simulation details are provided in the methods section and Figure S9 in the supplementary material. The simulated structure includes a 100 nm SiO₂ capping layer which aims to prevent evaporation and deformation of the GST layer during melting. Alternatively, the structures can be formed by depositing the GST film on a glass substrate followed by the metal deposition to protect the GST layer (Figure S8 in the supplementary material). In this case, the surfaces show similar reflection spectra with a slight red-shift. The simulated structure uses Au with a higher melting temperature instead of Al. The simulation results suggest that both crystallization and melting temperatures can be achieved using appropriate electrical pulses (Figure 5(b)). Amorphization requires quenching after melting which necessitates the cooling time constants to be short, and hence the pixel structures to be small. The results show that for the modelled pixel size $(5 \times 5 \ \mu m^2)$, short heating/cooling time constants of ~ 100 ns can be realized (Figure 5(c)). Although, the GST volume which needs to be annealed for this operation is larger than typical PCM cells, SET and RESET operations have been demonstrated for even larger scale phase-change RF switches.³³ The proposed color pixel structure is tested by fabricating an array of Al wires with small dimensions $(2 \times 2 \mu m^2)$ and coating them with 20 nm aGST. The initial surface color is tuned by passing electric current (100 mA) through the wires and annealing the GST patch on top of the wires (Figure S10 in the supplementary material). The non-uniform temperature distribution and high current levels estimated by the measurements and simulations can be overcome with smart designs

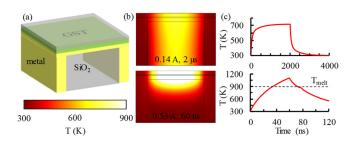


FIG. 5. Electrothermal simulation results. (a) Illustration of the simulated pixel structure. SiO_2 layers are shown semi-transparent for clarity. (b) Temperature distributions on the 2D structure at the end of electrical pulses applied for crystallization (top) and amorphization (bottom). (c) Evolution of the peak temperature in the GST film during and following the crystallization and amorphization pulses.

and materials, such as serpentine heater structures, highresistivity reflective materials, and better thermal isolation.

In summary, we observe that thin GST layers on metals, such as Al, Ag, and Au produce colors owing to strong interference effects in the visible. A color scale ranging from yellow to red to blue that is produced with different thicknesses of GST on Al layers changes to dim gray upon crystallization of the GST film by annealing. The surfaces show angleindependent optical responses as confirmed by the reflection measurements and perceived by the naked eye. Introducing a lossless dielectric (HfO₂) layer between the metal and GST layers enables further tuning of the optical response by exciting the Fabry-Pérot modes. The narrow Fabry-Pérot resonances which can be tuned by the dielectric thickness offer a rich color gamut which can be shifted by crystallization of the GST layer. Finally, the possibility of forming a display is assessed through electrothermal modeling of a pixel structure consisting of a SiO₂/GST/metal stack. The metal layer acts as a reflector as well as a heater for uniform heating of the atop GST film. Simulation results for a pixel element with 20 nm GST on 80 nm metal layer and 5 \times 5 μ m² area show that the temperature levels and quenching time required for amorphization can be achieved. Such a pixel structure capable of thermal color tuning can enable highresolution, non-volatile, large-area, rewritable displays.

See supplementary material for fabrication, measurements, and simulations details, optical constants of the materials, additional optical measurement results, and demonstration of a color pixel.

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