Optimal fiscal decentralization: Redistribution and welfare implications

Erkmen Giray Aslim\textsuperscript{a}, Bilin Neyapti\textsuperscript{b,⁎}

\textsuperscript{a} Lehigh University, Department of Economics, Bethlehem, PA 18015, USA
\textsuperscript{b} Bilkent University, Department of Economics, Bilkent, Ankara 06800, Turkey

\textbf{A R T I C L E  I N F O}

\textbf{JEL codes:}
E62
H77

\textbf{Keywords:}
Fiscal decentralization
Welfare
Fiscal efficiency
Income distribution

\textbf{A B S T R A C T}

The literature has been inconclusive regarding the welfare effects of fiscal decentralization (FD), defined here as the extent to which local governments collect and spend local tax revenues. We present an original model to investigate formally the distributional and welfare implications of FD. In contrast to the standard approach that compares the implications of full FD with that of centralization, we consider that the central government chooses the level of FD to maximize welfare in a heterogeneous country. Noncooperatively, local governments choose their tax collection effort to maximize local utility. We show that an increase in the tax rate leads optimal FD to increase so as to compensate for the welfare loss from decreasing optimal local tax effort. Hence, welfare and income distribution improve in FD at its intermediate, rather than extreme, levels. We coin this result as the decentralization-Laffer curve. As regional spillovers increase, FD is less desirable as it deteriorates welfare and income distribution. This finding provides a novel support for the decentralization theorem and contributes to the fiscal policy debate.

\section{1. Introduction}

Fiscal decentralization (FD), defined as the devolution of fiscal power and responsibilities to sub-national governmental units, has been argued to improve democratic governance practices and thus to contribute to asymmetric or incomplete information, that put local provision is welfare-enhancing especially when regions are heterogeneous main policy implication that follows the centralization theorem. The literature has paid to the decentralization theorem. Notwithstanding the considerable attention

\footnote{⁎ Corresponding author.}

\textsuperscript{a} An inspection of the Fiscal Decentralization Indicators of the World Bank reveal the following stylized facts: i) federal systems generally have greater degrees of FD than the rest; ii) developed countries are associated with higher levels of FD than less developed countries (see Neyapti (2010)); iii) expenditure decentralization is higher than revenue decentralization in both developed and developing countries; and iv) there are varying degrees of vertical and horizontal imbalances in each country.

\textsuperscript{b} Following Tiebout’s (1956) seminal work, there has been a growing literature on FD. See, for example, Oates (1972, 1998, 1999), Prud’homme (1995), and Diamond (1999) to name a few.

\textsuperscript{c} See, for example, Prud’homme (1995), Stein (1998), Alesina et al. (1999), Rodden (2002), Tanzi (1994), and Fisman and Gatti (2000).

\textsuperscript{d} See, for example, Burki et al. (1999), Tanzi (2000), De Mello and Barenstein (2001) and Neyapti (2010, 2013), on the importance of various attributes of governance mechanisms for FD to be associated with improved economic outcomes. Using the IMF measures of fiscal rules across countries, Neyapti (2013) demonstrates that increasing FD is associated with lower fiscal deficits in case of fiscal rules. Sanguinetti and Tomassi (2004), Stowhase and Traxler (2005), Akin et al. (2014), and Neyapti and Bulut-Cevik (2014) all show that rule-based transfer mechanisms improve fiscal efficiency.
nor desirable to decentralize public activity entirely; hence an intermediate level of FD is preferable for improving welfare or fiscal discipline.\textsuperscript{3}

The existing studies that formally model FD generally compare the outcomes of fully centralized and decentralized fiscal structures. Lockwood (2002), for example, investigates the effects of distributive policies in a political economy model with externalities, and argues that, in contrast with Oates (1972), weaker externalities may not increase the efficiency gains from decentralization, depending on the nature of heterogeneities.\textsuperscript{4} Also in a political economy framework, Besley and Coate (2003) investigate the roles of spillovers and homogeneity for public good provision in cases of centralized and decentralized systems. They show that, due to cost sharing, decentralization may be superior to centralization even when spillovers are small and regions are homogeneous. Bellofatto and Besfamille (2015) compare the cases of partial and full decentralization with a focus on local fiscal and administrative capacity. Kothenbuerger (2008) investigates the welfare differentials of FD and centralization under spillovers and state the conditions that support the decentralization theorem. An important exception is Janeba and Wilson (2011) who state, also in a political economy model, that tax competition restricts the efficiency of decentralization, and show that an intermediate level of decentralization is optimal.

To our best knowledge, the literature has not yet provided a formal study of the welfare and redistributive implications of the optimal choice of the degree of FD in view of heterogeneous localities and spillover effects. The current study presents a framework where the extent to which the local revenue base is to be utilized locally is decided optimally by the central government, in a strategic interaction with local governments. It also investigates how structural and economic factors, specifically the prevailing tax rate and the share of the public sector vis-à-vis the private sector in the utility function affect optimal FD.

The model assumes three types of goods in each locality: local private good, local public good and pure public good. Assuming that the economy is closed, the central government (G) maximizes social welfare by choosing the degree of FD, which is assumed to be uniform across localities.\textsuperscript{5} The model is solved as a non-cooperative game between local governments (LGs) and G, where a representative LG chooses its relative tax collection effort, which determines the level of local public good. Given the complexity of the set-up, output is assumed to be given exogenously and the model is static.

The solution of the model reveals that an increase in the tax rate leads to an increase in optimal FD, but a decrease in the optimal tax collection effort, as well as in the effective tax rate. Given the feasible range of parameter values, maximum values of welfare and tax revenue correspond to a medium range of optimal FD values. In addition, income distribution improves for the medium range of optimal FD values. Hence, the paper’s findings caution the policy makers against a full-fledged and unconditional fiscal decentralization.

As an extension of the benchmark model, we investigate the optimal choice of FD when local public good provision has positive or negative spillover effects. The solution of the model reveals that spillovers have a positive effect on optimal FD and negative effect on tax collection effort, which appear to challenge the main argument of the decentralization theorem that state that spillovers reduce the welfare gains of FD. However, simulations also show that, when both income distribution and welfare effects are taken into account, lower rates of FD is preferable than in the case of no spillovers.

The structure of the rest of the paper is as follows. Section 2 describes the model as a strategic game between the central government and the local governments, Section 3 provides the comparative statics and simulation results, Section 4 extends the model to incorporate spillover effects, and Section 5 concludes.

2. The model

We consider a closed economy where the initial income of each region \((Y_i)\) is predetermined. We treat the private sector as a passive agent so as to focus on the interrelationship between the central and local governments. The level of spending in locality \(i\), denoted by \(V_i\),\textsuperscript{8} is given by the sum of private (\(C_i\)) and public spending that is composed of local and central government spending, denoted by \(G_i^L\) and \(G_i^C\), respectively.\textsuperscript{9} Because \(G_i^C\) is pure public good, it can be written that \(G_i^C = G^C_i\). The current framework is static; hence \(C_i\) is equal to the after-tax income as there is no capital accumulation:

\[
\bar{Y}_i = C_i + G_i^L + G_i^C
\]  

(1)

where

\[
C_i = (1 - \phi)Y_i, \quad G_i^L = \phi a_i Y_i, \quad \text{and} \quad G_i^C = (1 - \phi)\sum_i Y_i.
\]  

(2)

For the tractability of the model, we assume that the only tax base is income, from which both the local and the central governments collect taxes. \(t_i\) is the tax rate faced by region \(i\) \((i=1, \ldots, n)\) and it is equal to the sum of taxes collected by the local and the central governments:

\[
t_i = [a_i \phi + \tau (1 - \phi)]
\]  

(3)

where \(a_i\) is the relative tax collection effort (or capacity) of LG vis-à-vis the central government in region \(i\). \(\phi\) is the level of fiscal decentralization \((\phi \in [0, 1])\) that stands for the share of the local government in both total tax-revenue collection and public spending.\textsuperscript{10} The first component of \(t_i\), \(a_i\phi\), is the portion of tax revenue that is collected by LG\(_i\) and constitutes the sole source of financing for local public spending \((G_i^L)\);\textsuperscript{11} given \(a_i\), \(a_i\phi\) is the effective tax rate of LG\(_i\). The second component of \(t_i\), \((1 - \phi)\), the portion of local taxes that is collected by G and spent as \(G^C\), is consumed in equal amounts by each locality. Hence, \(G_i^L\) stands for a positive transfer to region \(i\) if \((1 - \phi)Y_i < G^C\).\textsuperscript{12} All variables are expressed in per capita terms. \(t\) is the constant average income tax faced by a representative agent in each region, and is assumed to be given exogenously.\textsuperscript{13}

The regions are assumed to be homogeneous in all respects other than their initial incomes, hence, the model focuses on a representative LG. There is no tax competition. We first solve for the benchmark case of \(n=2\), where G and LGs act non-cooperatively to determine the optimal levels of \(\phi\) and \(a_i\), respectively, given \(t\).

\textsuperscript{8} Total spending (\(\bar{Y}_i\)) differs from income (\(Y_i\)) by the amount of (positive or negative) transfers made by the central government. However, for the whole economy, the government budget is in balance, hence: \(\sum Y = \sum \bar{Y}_i\).

\textsuperscript{9} One may consider \(G^L_i\) as the local public good.

\textsuperscript{10} For simplicity, \(\phi\) is assumed to be invariant across regions.

\textsuperscript{11} One could model local spending to result from joint projects of the local and central governments. The large extent of nonlinearities already existing in the model, however, lead us to exclude this option for purposes of clarity in presentation.

\textsuperscript{12} Both regions receive positive transfers when \(t > 0\) and \(\phi > 0\) for all \(i\).

\textsuperscript{13} No explicit solution can be found to the problem where G optimizes both \(\phi\) and \(t\) due to the highly non-linear constraints of the model. An optimal solution for both \(\phi\) and \(t\) can be found, however, under the leader-follower type game as the corner solution, where \(\phi^* \equiv 1, a_i^* \equiv 0\); and \(\tau^* \equiv 0\). This solution, however, is not economically intuitive.
Both players are best responding to each other by acting strategically and the joint solution of their best response functions yields the Nash equilibrium. This framework is similar to Cournot’s duopoly model (see, for example, Daughety, 1989). The social planner’s problem yields the same optimal results as in this solution procedure because of regional symmetry assumption.\(^{14}\)

### 2.1. The local governments’ problem

The representative local government chooses its tax collection effort in order to maximize the local utility that is composed of both private and public (central and local) spending in the region. Local consumers and LG do not distinguish between G\(^2\) and G\(^C\) and hence receive the same level of utility from both.\(^{15}\) The utility function is concave and assumed to take the following log-linear form:

\[
\max_{a_i} U_i = \alpha \ln C_i + \beta \ln G_i^C + \beta \ln G_i^C.
\]

The first order condition of the problem subject to the constraints given in Eqs. (1) and (2) yields:

\[
a_i = \left( \frac{\beta}{\alpha + \beta} \right) \frac{1 - t^i + \phi^i}{\phi^i} - 1
\]

(5)

### 2.2. The central government’s problem

The government chooses \(\phi\) in order to maximize the social welfare, which is the unweighted sum of local utilities:

\[
\max_{\phi} \sum_i U_i = \sum_i \left( \alpha \ln C_i + \beta \ln G_i^C + \beta \ln G_i^C \right).
\]

(6)

Given the expressions in Eqs. (1) and (2), the problem yields the first order condition for \(i = 1, 2\):

\[
a_i \left( \frac{1 - a_i}{1 - t^i a_i} - t^i (1 - \phi) \right) + 1 - a_i = 0
\]

(7)

which, using symmetry, is equal to:

\[
2a_i \left( \frac{1 - a_i}{1 - t^i a_i} - t^i (1 - \phi) \right) + 2\beta \left( \frac{1}{\phi} - \frac{1}{1 - \phi} \right) = 0
\]

(8)

**Lemma 2.1.** LG’s best response function implies that \(\phi\) and \(a_i\) are substitute strategies whereas for \(G\) they are strategic complements.

**Proof.** We need to show that the derivative of \(a_i\) with respect to \(\phi\) is non-increasing in the LGs’ problem, and the derivative of \(\phi\) with respect to \(a_i\) is non-decreasing in the G’s problem. In the LGs’ problem, \(\frac{\partial \phi}{\partial a_i} = \left( \frac{t - 1}{1 - t} \right) \frac{1}{(\phi)^2} \leq 0\) holds for \(t \in [0, 1]\). For the G’s problem, applying the implicit function theorem to Eq. (8) yields:

\[
\frac{\partial \phi}{\partial a_i} = \frac{-2(1 - \phi + a_i)(1 - \phi + a_i) - 2\beta t(1 - \phi + a_i) + 1 - \phi}{(1 - \phi + a_i)^2},
\]

which is non-negative for \(t, \phi \in [0, 1]\).

**Lemma 2.2.** The joint solution of Eqs. (5) and (6) yields the optimal values for \(\phi\) and a representative \(a_i^*\):

\[
\phi^* = \left( \frac{a^* - \beta + 2\beta t}{a^* + 2\beta t} \right) \quad \text{and} \quad a_i^* = \frac{-\beta}{\beta - t(\alpha + 2\beta)}
\]

(9)

**Proof.** See Appendix A.

For a given set of feasible values of \((\alpha, \beta, t)\), the above solutions yield single values for \(\phi^*\) and \(a_i^*\), which implies that the joint solution of the problem exists. In addition, the proof of Lemma 2.1 shows that the best response functions intersect at a single point, which ensures that the equilibrium is unique.

In a Stackelberg framework, where we model the relationship between G and LG sequentially, we let G to be the first mover and choose \(\phi\) and LG to follow by choosing \(a_i\). This setup yields the same optimal values as those found in Eq. (9). Hence, the first-mover advantage does not exist.\(^{16}\)

**Lemma 2.3.** \(\phi^*\) and \(a_i^*\) are both feasible for \(t > \frac{1}{\alpha + 2\beta} = \frac{1}{\alpha + 2\beta} \).

**Proof.** For \(a_i^* \geq 0\), the necessary condition is: \(t < \frac{\left( \frac{\beta}{\alpha + 2\beta} \right)}{\left( \frac{\beta}{\alpha + 2\beta} \right)} \).

For \(\phi^* \in (0, 1)\), the constraint is: \(0 < \phi^* < t(\alpha + 2\beta)\), which is the same condition for \(a_i^*\).\(^{17}\)

This condition implies that \((\alpha, \beta)\) increases, the minimum value of \(t\) decreases to obtain the feasible range of the optimal values of the problem solution. To give a numerical example, the lower bound for \(t\) is 0.3 for \(\alpha = 0.5\), and 0.23 for \(\alpha = 0.7\) and \(\beta = 0.3\), for the feasibility of the solution. In the extreme case of \(\beta = 0\), \(a_i^*\) is zero and \(\phi^*\) is one, which is the case of full decentralization, implying no tax collection and no spending by the government. In the opposite case, the condition that ensures optimality of \(\phi\) is that it is equal to zero (or \(\beta = t\alpha + 2\beta\)), which is also the condition for \(a_i^*\) to go to infinity.

**Proposition 2.1.** The minimum tax rate for which the competitive (decentralized) solution obtains increases as the relative utility share of the government spending \((\beta/\alpha)\) increases.

An example to clarify the above observations can be given for the cases of France and the U.S.: expenditure decentralization is about 0.45 in the U.S., whereas it is about 0.20 in France.\(^{18}\) With the average tax rate (measured by the tax burden to GDP ratio) of 0.25 and the share of government spending of 0.39, the U.S. does not appear to have an optimal level of \(\phi\). The current level of \(\phi\) in the U.S. would be consistent, ceteris paribus, with a higher average tax rate, which is about 0.52 according to Eq. (9). For the case of France, where the average tax rate is about 0.45 and the government spending is about 0.22, \(\phi\) is approximately 0.23 according to Eq. (9), which is very close to the actual rate of 0.20. This framework therefore suggests the existing rate of \(\phi\) in France is about the welfare maximizing rate.

### 3. Comparative statics

This section further examines the non-cooperative solution of the optimal decisions of LGs and G. Comparative statics reported below are based on the closed form solutions (see Appendix B):

\[
\frac{\partial \phi^*}{\partial t} > 0; \frac{\partial \phi^*}{\partial a_i} > 0; \frac{\partial \phi^*}{\partial \beta} < 0; \frac{\partial a_i^*}{\partial t} < 0; \frac{\partial a_i^*}{\partial \alpha} < 0; \frac{\partial a_i^*}{\partial \beta} > 0
\]

(10)

The following explanations can be provided. First, the positive relationship of \(\phi^*\) with \(\beta\)\(^{19}\) arises because it is optimal for G to increase \(\phi\) to compensate for the reduction in \(a_i^*\). LGs’ optimal response to an increase in \(t\) is to reduce \(a_i^*\) so as to compensate for the utility loss from a decrease in the disposable income, which reduces the utility from private consumption. The positive association between \(\phi^*\) and \(t\) is consistent with the empirical evidence, for example, for the case of China (Qichun, 2014).

\(^{14}\) The solution is available from the authors upon request.

\(^{15}\) We assume that government spending in a given locality generates local public good, whose source does not matter; undirected transfer spending would justify this assumption.

\(^{16}\) The result is different, however, when we introduce spillovers.

\(^{17}\) This specification is defined to avoid corner solutions as it is discussed earlier.

\(^{18}\) The numbers are rounded up. FD indicators are obtained from the World Bank, and the tax burden to GDP ratio is obtained from the Economic Freedom Index of the Heritage Foundation.

\(^{19}\) The positive response of \(\phi\) is decreasing in \(t\)
Proposition 3.1. $\phi^*$ increases in $t$ and $a_1^*$ decreases in $t$.

Proposition 3.1 indicates that the effect of an increase in $t$ on local tax revenue can be ambiguous and a tax-Laffer curve may or may not exist. We investigate this issue with the help of simulations in the next section.20

The comparative statics also indicate that optimal $\phi$ is positively related with the share of the private sector ($a$). It is also observed that the sign of the relationships between $a^*$ and $\alpha$, and $a^*$ and $\beta$, are negative and positive, respectively. This is because increasing $a^*$ reduces disposable income, which reduces local utility more the higher the relative utility share of the private sector ($a/\beta$). Therefore, as $a$ gets higher, LGs prefer to exert less effort to collect taxes.

Proposition 3.2. The higher is the ratio ($a/\beta$), the higher is $\phi^*$.

3.1. Simulations and numerical examples

In this section, we investigate the interactions of the optimal choices of $(a; \phi)$ with the rest of the model variables $(C, G, \beta, a_1^*, 1, \tilde{Y}$, $U^L$ and $U^G$) and the parameters $(a; \beta$ and $t$), where $U^L$ and $U^G$ denote the levels of utility pertaining to LG and G. We refer to $U^L$ as “welfare”. Further, we investigate the relationship of $(a^*; \phi^*)$ with income distribution $(h/i)$.

To obtain numerical solutions, we assign values to the model parameters as follows: $(a; \beta; t) \in [0, 1]$. We also fix one region’s income and define the other region’s income as a multiple $(x)$ of that, where $x$ varies over the range of $[1, 10]$, which means that the income level in one region can be as small as one-tenth of the other region. Numerical simulations are performed covering all the feasible ranges of the underlying model parameters, where $a_1^* \in \mathbb{R}_+$; $\phi^* \in [0, 1]$; and $(C, G, C^*, G^*, Y, \tilde{Y}) \in \mathbb{R}_+$. The simulations generate 5,520 data points, an example of which is provided in Appendix C. Based on these, the following observations can be made:

i. Appendix C presents a numerical example of the simulation results. It demonstrates that income distribution improves as $\phi^*$ decreases, for a given $t$, corresponding to an increase in $\alpha$ (and a decrease in $\beta$). In response, income distribution $(\tilde{Y}/Y)$ takes the values of 1.53 and 1.40, respectively, as opposed to the initial ratio of 2. This reflects that the redistributive role of the G decreases with $\phi^*$.21 In addition, we observe that the effective tax rate increases in the relative utility share of the public sector $(\beta/\alpha)$.22

This numerical example is only suggestive, however. A broader picture of the effects of $\phi^*$ can be seen based on the plots of the whole dataset generated by the simulations. Those plots are shown in Appendix D, which we turn to next.

ii. Fig. 1 shows that the possible range of income distribution, corresponding to the set of alternative parameter values, is most equitable in the case of $\phi^* = 0.5$. The data plots on the horizontal axis correspond to the initial values of $Y_1 = Y_2 = 10$, which implies no redistribution and hence $Y_1/Y_2$ remains as 1 for the whole range of $\phi^*$. Fig. 2 shows that total tax collection effort is inversely related with $\phi^*$. This is consistent with the negative and positive definite comparative statics of $t$ with the former and the latter, respectively.

iii. Fig. 3 shows that the highest level of tax revenue is associated with an intermediate value of $\phi^*$. Because optimal tax effort declines in $\phi^*$ and $t$, the range of tax revenues shows a positive relationship with $\phi^*$ for $\phi^* < 0.5$; and a negative one for $\phi^* > 0.5$. This may be called as the decentralization-Laffer curve, which shows an inverted-U relationship between $\phi^*$ and tax revenues.

iv. Accordingly, Fig. 4 shows that tax revenues first increase and then decrease in $a_1^*$. This is because $a_1^*$ falls in $t$, which in turn increases the tax revenue. However, we do not observe the falling portion of the tax-Laffer curve (see Fig. 5), which implies that the choice of $\phi^*$ is such that its rise in $t$ overcomes the negative effect of an increase in $t$ and $a_1^*$.

v. Fig. 6 shows that welfare is also maximized for a medium range of optimal $\phi$ values. Specifically, the highest values of welfare are obtained for $0.4 < \phi < 0.7$.

vi. Based on Fig. 7, we observe that the range of welfare reaches its highest levels when income distribution is at reasonably equitable levels (specifically, for $Y_1/Y_2 < 2.5$). Similar to Fig. 1, the values on the vertical axis correspond to the case of no redistribution.

These findings indicate, in a nutshell, that both welfare and income distribution reach their best points for a median range of $\phi^*$ values. This is consistent with the recent literature that argues that extreme

20 This finding is consistent with the literature. See, for example, Adam et al. (2014) for the empirical analysis of the relationship between FD and the efficiency of public education and health spending in the OECD countries, where the authors show an inverted-U relationship.

21 If $\phi^* = 1$, no redistribution takes place and post income distribution is either 2 or 0.5 as reflected by the initial values of $Y_1$ and $Y_2$.

22 Under the assumption that the share of the private sector consumption in utility is 0.7 and that of the public sector is 0.3, simulations for $\phi^* = 0.5$ reveal that the effective tax rate faced by LGs ($\omega t$) is 0.46 which is consistent with developed country average (see Appendix C). The de-facto effective tax rate ($\omega a\phi$) is, on the other hand, 0.26.
values of FD is not desirable for welfare and efficiency reasons (see, for example, Thiessen, 2003; Neyapti, 2010; Wang, 2013 among others).23

4. Extension: spillover effects

The benchmark model analyzed above allows for regional heterogeneity only in income levels. It is common, however, that local administrations take such actions that have effects on the welfare of other localities. These externaties may be in the form of influencing other localities’ tax collection capacities and public spending needs. Positive spillovers may arise from infrastructure or education spending. An investment on a chemical plant, for example, may spillover negatively by polluting the environment and reducing tourism in a neighboring region, however. Tax exporting is another form of negative spillovers (see, for example, Boadway and Shah, 2009; Sorens, 2014).

In this section, we consider that local public spending may exert varying degrees of spillovers across the regions. According to Oates...
spillovers may result in the underprovision of the local public goods and hence decentralization becomes less justified, a view that is challenged by Lockwood (2002) in a political economy context. In order to investigate how spillovers may alter the findings of our model, we modify the LGs’ utility function as:

$$\max_{a_i} U_{\text{spillover}} = a_i \ln C_i + \beta (\ln C_i^s + s_i \ln C_i^f) + \beta \ln C_i^r.$$  (11)

where $s_i \in [-1, 1]$ stands for the degree of spillover of region $j$’s public spending on region $i$. Two cases may arise under this specification: under one, the information about spillovers is observed only by the locals, and not by G; this is the case of asymmetric information. In this case, we observe that the LGs’ first order condition does not contain $s_i$ and thus is the same as the one reported in Eq. (9). Because the optimal solution for $\phi$ also remains the same as those reported above, the distributional and welfare effects also remain the same as under no spillover effects.

Under the alternative case, when G has the full information about the spillovers, the G’s problem becomes:

$$\max_{\phi} \sum_{i} U_{\text{spillover}} = \sum_{i} (a_i \ln C_i + \beta (\ln C_i^s + s_i \ln C_i^f) + \beta \ln C_i^r).$$  (12)

We solve the problems given in Eqs. (11) and (12), subject to the constraints given in Eqs. (1) and (2), both as a simultaneous and sequential move games, which are reported in Sections 4.1 and 4.2.

4.1. Simultaneous move game

Under full information about local spillovers, the first order conditions of the non-cooperative solution to the above problem is given by:

$$\frac{\partial U_{\text{spillover}}}{\partial a_i} = \frac{-a_i \beta (1 - \phi) + \beta (2 + s_i)}{1 - \phi a_i}, \quad \frac{\partial U_{\text{spillover}}}{\partial \phi} = \frac{\beta (2 + s_i)}{\phi} - \frac{2 \beta}{1 - \phi} \leq 0.$$  (13)

The joint solution of these first order conditions yields two distinct roots for $\phi^*$ and $a_i^*$ that are too long to report here. The comparative statics of those solutions are also too long to report; hence the signs are obtained through numerical simulations that cover all feasible ranges of the parameter values, in addition to the assumption about the range of spillovers: $s_i \in [-1, 1]$. Based on the simulations, we observe that the effects of spillovers on $\phi^*$ and $a_i^*$ are: $\partial \phi_{\text{spillover}}/\partial \phi \geq 0$ and $\partial a_{i,\text{spillover}}/\partial \phi \leq 0$. The non-zero values of the derivatives are observed to be very few, however, and are available mostly for negative spillovers ($s_i \in [-1, 0]$). Hence, we conclude that the derivatives are not well-defined in this scenario.

We next investigate the relationship of $\phi^*$ with welfare and income distribution under spillovers. The most striking result we observe is that decentralization-Laffer curve disappears in the case of spillovers; that is, the intermediate range of $\phi^*$ values do not correspond to the highest levels of tax revenue anymore. Accordingly, income distribution and FD relationship is almost reversed as compared to the benchmark case: income distribution worsens as $\phi^*$ gets close to 0.5, from above and below that point; while it is observed to improve as $\phi^*$ decreases, reaching the most equitable levels at $\phi^* \approx 0.1$. By contrast, the highest attainable levels of welfare correspond to more extreme values of $\phi^*$ ($\phi^* \geq 0.7$) than the benchmark case. In view of these numerical simulation results, a benevolent government facing large regional spillovers would have to consider the trade-off between welfare and income distribution: if equitable distribution of income is viewed more important than increasing welfare, a low level of FD would be optimal. This observation is consistent with the decentralization theorem.26

The numerical examples in Appendix E also show that increasing spillovers have a positive effect on $\phi^*$ (compare the first two columns of Appendix E, and the first column of Appendix C to that in Appendix C) and result in worse income distribution than the benchmark case reported in Appendix C. In addition, increasing spillovers is observed to lead to worse income distribution (compare 1.58 to 1.67, or 1.50 to 1.62 in Appendix E).

4.2. Sequential move game

In an alternative scenario, where spillovers are common knowledge to both LG and G, G moves first and sets $\phi$ taking LG’s reaction function into account. LG in turn, chooses $a_i$ by optimally taking $\phi$ given. This scenario is plausible considering that $\phi$ can be treated as a predetermined institutional variable according to which LGs take their actions. The first order conditions of the LG and G problems of this scenario are:

$$\frac{\partial U_{\text{spillover}}}{\partial a_i} = \frac{-a_i \beta (1 - \phi) + \beta (2 + s_i)}{1 - \phi a_i}, \quad \frac{\partial U_{\text{spillover}}}{\partial \phi} = \frac{\beta (2 + s_i)}{\phi} - \frac{2 \beta}{1 - \phi} \leq 0.$$  (14)

**Lemma 4.1.** The joint solution of Equations in (14) yields the non-cooperative optimal values for $\phi$ and $a_i$: $\phi^*_{\text{spillover}} = 1 - \frac{\beta}{(a + \beta(2 + s_i))}$ and $a^*_{i,\text{spillover}} = \frac{\beta(a + \beta s_i)}{\phi(a + \beta(2 + \beta s_i))}$.  (15)

**Lemma 4.2.** $\phi^*_{\text{spillover}}$ and $a^*_{i,\text{spillover}}$ are feasible ($0 < \phi^*_{\text{spillover}} < 1$ and $0 < a^*_{i,\text{spillover}} < 1$) when $\beta > 0$.27

Comparative statics of the optimal solutions with respect to $[\tau, \alpha, \beta]$ yield the same results as those reported earlier for the benchmark case. The following results are additional28:

$$\frac{\partial \phi^*_{\text{spillover}}}{\partial \beta} > 0 \quad \text{and} \quad \frac{\partial a^*_{i,\text{spillover}}}{\partial \beta} < 0.$$  (16)

which reveals a strictly positive relationship between $s_i$ and $\phi^*$, unlike the non-sequential game between G and LG under spillovers; that is, negative spillovers reduce $\phi$ and positive spillovers increase it definitively. These results are also observed to be much more robust than the former case because they are defined for the whole range of $s_i$s.

These findings appear to challenge the decentralization argument by Oates (1972): the presence of spillovers actually makes the case for decentralization stronger. The simulations show, however, that the range of $\phi^*$ values at which welfare reaches its maximum values are about the same as the case without spillovers: some intermediate range of the $\phi^*$ values (specifically, $0.4 < \phi^* < 0.7$), although the lower tail of $\phi^*$ is observed to be associated with higher levels of welfare than in the benchmark case (as in Section 4.1).

---

24 The solution functions are available from the authors upon request. Of the two roots of optimal $\phi$, only the first yields data for the whole range of $\phi^*$; hence, the analysis is based on the first root only.

25 For one of the roots, for which model produces feasible outcomes only for $\phi^* < 0.5$, welfare is also observed to increase as $\phi^*$ gets smaller. Data and graphs are available upon request from the authors.

26 Decentralization theorem suggests that centralization can be justified when local governments do not internalize the externalities or when there are large spillovers.

27 For $\beta = 0$, $\phi^*_{\text{spillover}} = 1$ and $a^*_{i,\text{spillover}} = 0$, which is not feasible as discussed earlier.

28 The proof is trivial.

29 This result is consistent with that of Koethenbuerger (2008) who shows that increasing spillovers reduces the welfare differences between FD and centralization.
On the other hand, decentralization-Laffer curve disappears (as in Section 4.1): tax revenue increases as $\phi^*$ falls and income distribution improves as $\phi^*$ approaches to the value of 0.1. The remainder of the observations, namely with regards to the tax-Laffer curve, depicted in Appendix D for the case of no spillovers remains virtually the same.

Hence, the simulation results appear to be at odds with the comparative statics result that shows $\phi^*$ to increase in spillovers. The lowest levels of $\phi^*$ are associated with the highest attainable levels of redistribution (tax revenue) under spillovers, in contrast with the case of no spillovers. The following explains why these findings are actually not contradictory. Spillovers affect local utility through $G^2i's$ that increase in both $\phi$ and $a_i$, which, however, are negatively related with each other. When spillovers increase, if $\phi^*$ was to increase and $a_i^*$ was to fall as much as in the benchmark case, utility from $G^2i's$ would still rise due to spillovers. It is therefore possible that welfare reaches highest attainable levels at lower levels of $\phi^*$ than in the benchmark case. The intuition can be further explained in case of a decrease in spillovers: because G knows that $a_i^*$ will increase in response, $\phi^*$ falls by more than the benchmark case (so that $t_i$ in Eq. (3) falls) in order to eliminate the utility loss from a reduction in $C_i$.

The findings are therefore consistent with the comparative static result that seems to challenge the decentralization theorem: as spillovers rise, $\phi^*$ increases. However, since the welfare measure adopted here, which is the sum of local utilities, does not tell anything about the income distribution resulting from the model’s solution, a sound policy recommendation calls for a careful interpretation of the above results, which is as follows. If a benevolent government that faces regional spillovers considers both the welfare and income distribution implications of its choice, it would choose a low level of $\phi$ because it achieves larger redistribution without compromising much the level of welfare. From that perspective, it is indeed optimal to choose lower $\phi$ for higher rates of spillovers.

5. Conclusion

This paper contributes to the literature of fiscal decentralization by presenting a formal model to analyze the macroeconomic implications of optimizing fiscal decentralization (FD). We consider a framework where local governments determine their effective tax rates by choosing the degree of their tax collection effort optimally while the central government chooses FD optimally. Our benchmark case is when both local and central governments form their optimal decisions simultaneously in a non-cooperative fashion; we then also investigate the case of a sequential move game. Simulations are performed to assess the welfare effects of these interactions with and without the effect of spillovers across the regions.

The main finding of the paper is that it is optimal to increase the rate of fiscal decentralization (FD) the higher the tax rate so as to maintain the welfare level, given that the optimal local tax collection effort ($a_i^*$) decreases in the tax rate. Given the strategic complementarity between the optimal values of FD ($\phi^*$) and $a_i^*$, increasing $\phi^*$ first leads to an increase in the tax revenue and then decreases it. Simulations also show that optimum welfare reaches its highest values and income distribution becomes most equitable at some medium range of $\phi^*$. We call this decentralization-Laffer curve. This formal result makes a notable contribution to the recent decentralization literature stating that extreme values of FD may not be optimal. A tax-Laffer curve is not observed, however, since the optimal choices of the central and local governments avoid the realization of the falling portion of the curve.

Utilizing both non-sequential and leader-follower frameworks to solve the benchmark model in the case of spillovers, we observe that $\phi^*$ increases but $a_i^*$ decreases with spillovers, ceteris paribus. The extreme levels of $\phi^*$ are also associated with relatively low levels of welfare, as in the case of no spillovers, although the attainable range of welfare corresponding to lower levels of $\phi^*$ is relatively much higher than the benchmark case. In the presence of spillovers, revenue collection and income distribution improves uniformly as $\phi^*$ falls.

Taking stock, we conclude that when there are no spillovers, welfare and income distribution improves for a median range of values of fiscal decentralization. Extremely low and high values of FD lead to efficiency losses that results in low tax revenues to be utilized for redistributive purposes. In the presence of spillovers, however, the current framework reveals that low FD would be the preferred policy of a benevolent government if distribution of income matters as much as the level of aggregate welfare.

Acknowledgments

We thank the conference participants at EcoMod 2014 Meetings and the seminar participants at Bilkent University. We are also indebted to Cagri Saglam, Ernest Lai, James Dearden, two anonymous referees for their invaluable comments. In addition, we are grateful to the Editor of Economic Modelling for his valuable guidance and comments. All the remaining errors belong to the authors.

Appendix A. Model solution

I. Proof of LG’s First Order Condition (FOC). Substituting Eqs. (1) and (2) into (4) converts the problem into an unconstrained optimization as denoted below.

$$
\max_{a_i} U_i = a_i ln(Y_i - \phi a_i Y_i - (1 - \phi) a_i Y_i) + \beta ln(\phi a_i Y_i) + \beta ln\left(\sum_{i=1}^{n} ((1 - \phi) a_i Y_i)\right)
$$

from which the first order condition is obtained as:

$$
\frac{\partial U_i}{\partial a_i} = \frac{-a_i \phi Y_i}{Y_i - \phi a_i Y_i - (1 - \phi) a_i Y_i} + \frac{\beta \phi Y_i}{\phi a_i Y_i} = 0
$$

$$
a_i = \frac{\alpha}{\beta} \left(\frac{Y_i - \phi a_i Y_i - (1 - \phi) a_i Y_i}{\phi a_i Y_i}\right) = \frac{\alpha}{\beta} \left(\frac{1}{\phi^*} - a_i - \frac{1}{\phi^*} + 1\right)
$$

$$
a_i = \frac{\beta}{\alpha + \beta} \left(\frac{1}{\phi^*} - \frac{1}{\phi^*} + 1\right)
$$

For each jurisdiction ($i=1,2$), we have the same tax effort ($a_1=a_2$).
II. Proof of the G’s FOC. Substituting Eqs. (1) and (2) into (6) converts the model into an unconstrained optimization given by:

$$\max_{\phi} \sum_{i=1}^{n} U_i = \alpha \sum_{i=1}^{n} \ln(Y_i - \phi a_i Y_i - (1 - \phi) t Y_i) + \beta \sum_{i=1}^{n} \ln(\phi a_i Y_i) + \beta \sum_{i=1}^{n} \ln\left(\sum_{i=1}^{n} (1 - \phi) t Y_i\right)$$

whose first order condition is:

$$\frac{\partial}{\partial \phi} \sum_{i=1}^{n} U_i = \alpha \sum_{i=1}^{n} \left(\frac{1}{Y_i - \phi a_i Y_i - (1 - \phi) t Y_i}\right) + \beta \sum_{i=1}^{n} \left(\frac{1}{\phi a_i Y_i}\right) + \beta \sum_{i=1}^{n} \left(\frac{-1}{(\sum_{i=1}^{n} (1 - \phi) t Y_i)}\right)$$

which can be simplified as:

$$\alpha \sum_{i=1}^{n} \left(\frac{1 - \phi}{1 - \phi a_i t - (1 - \phi) t Y_i}\right) + n \beta \left(\frac{1}{\phi} - \frac{1}{1 - \phi}\right) = 0.$$  

For two jurisdictions ($i=1,2$), the solution is given by:

$$\alpha \left(\frac{1 - \phi}{1 - \phi a_i t - (1 - \phi) t Y_i} + \frac{1 - \phi}{1 - \phi a_2 t - (1 - \phi) t Y_2}\right) + 2 \beta \left(\frac{1}{\phi} - \frac{1}{1 - \phi}\right) = 0$$

This expression yields three roots for $\phi$; we only use this general solution for Lemma 2.1.

III. Proof of Lemma 2.2. Given two jurisdictions, substituting Eq. (5) in (8) yields:

$$2 \alpha \left(\frac{1}{\alpha + \beta} - \frac{1}{\alpha + \beta} (1 - \phi) t - \frac{\beta (1 - \phi) t - (1 - \phi) t}{\alpha + \beta}\right) + 2 \beta \left(\frac{1}{\phi} - \frac{1}{1 - \phi}\right) = 0$$

which yields:

$$\beta \left(\frac{1 - 2 \phi}{-\phi (\phi - 1)}\right) + \alpha \left(\frac{1 - \phi}{\phi (\phi - 1)} - \frac{1}{\phi (\phi - 1)} (1 - \phi) t + \frac{1}{\phi (\phi - 1)} (1 - \phi) t + 1\right) = 0$$

which can be simplified as:

$$\beta \left(\frac{1 - 2 \phi}{-\phi (\phi - 1)}\right) + \frac{\beta t - \beta + \alpha \phi t}{\phi (\phi - t + 1)} = 0$$

which yields (where $0 < (\alpha, \beta, t, \phi) < 1$):

$$\phi = \frac{-\beta + \alpha t + 2 \beta t}{(\alpha + 2 \beta) t} \text{ and } (\alpha + 2 \beta) t \neq 0 \text{ and } \beta (\alpha + \beta) \neq 0.$$  

In order to obtain the corresponding optimal tax effort ($a_i$), we substitute this expression in Eq. (5):

$$a_i^* = \frac{\beta}{\alpha + \beta} \left(\frac{1}{\frac{-\beta + \alpha t + 2 \beta t}{(\alpha + 2 \beta) t}} + \frac{1}{\frac{-\beta + \alpha t + 2 \beta t}{(\alpha + 2 \beta) t}}\right) = \frac{\beta}{\alpha + \beta} \left(\frac{\alpha + 2 \beta}{-\beta + \alpha t + 2 \beta t} - \frac{(\alpha + 2 \beta) t}{-\beta + \alpha t + 2 \beta t} + 1\right) a_i^*$$

$$= \frac{\beta}{\alpha + \beta} \left(\frac{\alpha + 2 \beta - \beta + \alpha t + 2 \beta t - \beta + \alpha t + 2 \beta t}{-\beta + t (\alpha + 2 \beta)}\right)$$

Since efforts are the same for each locality,

$$a_i^* = a_i^* = \frac{-\beta}{\beta - t (\alpha + 2 \beta)}$$

E.G. Aslim, B. Neyapti
Economic Modelling 61 (2017) 224–234
Appendix B. Comparative static analysis

\[ \frac{\partial \phi^*}{\partial t} = \frac{\beta}{t^2(\alpha + 2\beta)} > 0, \quad \frac{\partial \phi^*}{\partial \beta} = -\frac{\beta}{t(\alpha + 2\beta)^2} < 0, \quad \frac{\partial \phi^*}{\partial \alpha} = \frac{\beta}{t(\alpha + 2\beta)^2} > 0, \quad \frac{\partial \phi^*}{\partial t} \frac{\partial \alpha}{\partial \beta} = \frac{-\beta}{t(\alpha + 2\beta)^2} < 0, \quad \frac{\partial \phi^*}{\partial t} \frac{\partial \beta}{\partial \alpha} = \frac{\beta}{t(\alpha + 2\beta)^2} > 0, \]

\[ \frac{\partial \phi^*}{\partial \alpha} = \frac{-\beta}{(\beta - t(\alpha + 2\beta))^2} < 0 \]

Appendix C. Numerical examples

\( t = \{0.4, 0.6\}; \quad \alpha = \{0.5, 0.7\}; \quad \beta = \{0.3, 0.5\}; \quad Y = \{10, 20\} \)

<table>
<thead>
<tr>
<th>Parameter values</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t )</td>
</tr>
<tr>
<td>( \alpha )</td>
</tr>
<tr>
<td>( \beta )</td>
</tr>
<tr>
<td>( Y_1 )</td>
</tr>
<tr>
<td>( Y_2 )</td>
</tr>
<tr>
<td>0.4</td>
</tr>
<tr>
<td>0.7</td>
</tr>
<tr>
<td>0.3</td>
</tr>
<tr>
<td>20</td>
</tr>
<tr>
<td>10</td>
</tr>
<tr>
<td>0.6</td>
</tr>
<tr>
<td>0.7</td>
</tr>
<tr>
<td>0.3</td>
</tr>
<tr>
<td>20</td>
</tr>
<tr>
<td>10</td>
</tr>
<tr>
<td>0.4</td>
</tr>
<tr>
<td>0.5</td>
</tr>
<tr>
<td>0.5</td>
</tr>
<tr>
<td>20</td>
</tr>
<tr>
<td>10</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Variables</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \phi^* )</td>
</tr>
<tr>
<td>( \alpha^* )</td>
</tr>
<tr>
<td>Effective ( t )</td>
</tr>
<tr>
<td>( C_1 )</td>
</tr>
<tr>
<td>( C_2 )</td>
</tr>
<tr>
<td>( GL_1 )</td>
</tr>
<tr>
<td>( GL_2 )</td>
</tr>
<tr>
<td>( t_{1L}^{LG} )</td>
</tr>
<tr>
<td>( t_{2L}^{LG} )</td>
</tr>
<tr>
<td>Welfare</td>
</tr>
<tr>
<td>Tax Revenue</td>
</tr>
<tr>
<td>( Y_1 )</td>
</tr>
<tr>
<td>( Y_2 )</td>
</tr>
<tr>
<td>( Y_{\text{Dist (post)}} )</td>
</tr>
<tr>
<td>0.42</td>
</tr>
<tr>
<td>1.36</td>
</tr>
<tr>
<td>0.55</td>
</tr>
<tr>
<td>10.77</td>
</tr>
<tr>
<td>5.38</td>
</tr>
<tr>
<td>4.62</td>
</tr>
<tr>
<td>2.31</td>
</tr>
<tr>
<td>2.70</td>
</tr>
<tr>
<td>2.01</td>
</tr>
<tr>
<td>4.71</td>
</tr>
<tr>
<td>20.77</td>
</tr>
<tr>
<td>22.31</td>
</tr>
<tr>
<td>14.62</td>
</tr>
<tr>
<td>1.53</td>
</tr>
<tr>
<td>0.62</td>
</tr>
<tr>
<td>0.63</td>
</tr>
<tr>
<td>0.38</td>
</tr>
<tr>
<td>10.77</td>
</tr>
<tr>
<td>5.38</td>
</tr>
<tr>
<td>4.62</td>
</tr>
<tr>
<td>2.31</td>
</tr>
<tr>
<td>2.70</td>
</tr>
<tr>
<td>2.01</td>
</tr>
<tr>
<td>4.71</td>
</tr>
<tr>
<td>20.77</td>
</tr>
<tr>
<td>22.31</td>
</tr>
<tr>
<td>14.62</td>
</tr>
<tr>
<td>1.53</td>
</tr>
<tr>
<td>0.17</td>
</tr>
<tr>
<td>5.00</td>
</tr>
<tr>
<td>2.00</td>
</tr>
<tr>
<td>6.67</td>
</tr>
<tr>
<td>3.33</td>
</tr>
<tr>
<td>6.67</td>
</tr>
<tr>
<td>3.33</td>
</tr>
<tr>
<td>3.05</td>
</tr>
<tr>
<td>2.36</td>
</tr>
<tr>
<td>5.40</td>
</tr>
<tr>
<td>30.00</td>
</tr>
<tr>
<td>23.33</td>
</tr>
<tr>
<td>16.67</td>
</tr>
<tr>
<td>1.40</td>
</tr>
</tbody>
</table>

Appendix D. Simulations

\( (\alpha, \beta, t \in [0.1, 1]; \quad x \in [1, 10]; \quad y_2 = y_1) \) where the simulations pick the numbers from these ranges with 0.1 point intervals except for \( x \). The incremental change for \( x \) is 1 unit.\)
Appendix E. Numerical examples with spillover effects ($s_i$)

\[ t = \{0.4 \}; \alpha = \{0.5, 0.7\}; \beta = \{0.3, 0.5\}; Y = \{10, 20\} \]

<table>
<thead>
<tr>
<th>Parameter values</th>
<th>Simultaneous Move Game (1–4)</th>
<th>Sequential Move Game (5–8)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$t$</td>
<td>0.4</td>
<td>0.4</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>0.7</td>
<td>0.7</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.3</td>
<td>0.3</td>
</tr>
<tr>
<td>$Y_1$</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td>$Y_2$</td>
<td>10</td>
<td>10</td>
</tr>
</tbody>
</table>

$si = 0.2$

$si = 0.8$

$si = 0.2$

$si = 0.8$

Variables

<table>
<thead>
<tr>
<th>$\phi$</th>
<th>0.51</th>
<th>0.51</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a_i^*$</td>
<td>1.18</td>
<td>1.30</td>
</tr>
<tr>
<td>Effective $t$</td>
<td>0.47</td>
<td>0.52</td>
</tr>
<tr>
<td>$C_1$</td>
<td>11.27</td>
<td>10.91</td>
</tr>
<tr>
<td>$C_2$</td>
<td>5.63</td>
<td>5.46</td>
</tr>
<tr>
<td>$GL_1$</td>
<td>4.83</td>
<td>4.68</td>
</tr>
<tr>
<td>$GL_2$</td>
<td>2.41</td>
<td>2.34</td>
</tr>
<tr>
<td>$U_{1i}^{1G}$</td>
<td>2.75</td>
<td>2.75</td>
</tr>
<tr>
<td>$U_{2i}^{1G}$</td>
<td>2.10</td>
<td>2.10</td>
</tr>
<tr>
<td>Welfare</td>
<td>4.56</td>
<td>4.60</td>
</tr>
<tr>
<td>Tax Revenue</td>
<td>18.96</td>
<td>20.25</td>
</tr>
<tr>
<td>$Y_1$</td>
<td>21.95</td>
<td>22.21</td>
</tr>
<tr>
<td>$Y_2$</td>
<td>13.91</td>
<td>14.41</td>
</tr>
<tr>
<td>YDist(post)</td>
<td>1.58</td>
<td>1.54</td>
</tr>
</tbody>
</table>

$\chi (0.4), \gamma (0.5, 0.7), \zeta (0.3, 0.5), Y = (10, 20)$

Appendix F. Supplementary data

Supplementary data associated with this article can be found in the online version at http://dx.doi.org/10.1016/j.econmod.2016.12.008.

References

Economic Modelling 64 (2017) 224–234

233
Deficits in Latin America, Inter-American Development Bank and OECD, Washington, D.C.
Public Financ. 12, 515–531.