Benefits of transmission switching and energy storage in power systems with high renewable energy penetration

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HIGHLIGHTS

• A stochastic programming approach is proposed to model TS and ESS sizing simultaneously.
• The model considers DSM and renewable energy curtailment policies with various limits.
• The effect of TS on total cost, sizes, locations of ESS are discussed.
• We find that TS is noteworthy to analyze for power systems with renewable targets.

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ABSTRACT

Increasing the share of renewable energy sources in electricity generation helps address concerns about carbon emissions, global warming and energy security (i.e. dependence on fossil fuels). However, integrating intermittent and variable energy sources into the grid imposes new challenges for power system reliability and stability. To use these clean sources in electricity generation without endangering power systems, utilities can implement various control mechanisms, such as energy storage systems, demand side management, renewable energy curtailment and transmission switching. This paper introduces a two-stage stochastic programming model that co-optimizes transmission switching operations, and transmission and storage investments subject to limitations on load shedding and curtailment amounts. We discuss the effect of transmission switching on the total investment and operational costs, siting and sizing decisions of energy storage systems, and load shedding and renewable energy curtailment in a power system with high renewable penetration. An extensive computational study on the IEEE 24-bus power system with wind and solar as available renewable sources demonstrates that the total cost and total capacity of energy storage systems can be decreased up to 17% and 50%, respectively, when transmission switching is incorporated into the power system.

1. Introduction

1.1. Motivation

In the last two decades, the electricity industry experienced major changes. Increasing concerns about the environment and energy security reveal the necessity of using clean and sustainable energy resources in electricity generation. To encourage new investments to use more renewable energy sources (RESes), utilities implement policies such as feed-in tariffs, carbon taxes and/or renewable portfolio standards [1], and as a result, a 19% share of RESes in meeting world electricity demand in 2000 increased to 24% in 2016 [2]. Improvements such as this help reduce carbon emissions and dependence on fossil fuels. However, increased penetration of RESes can lead to high variability and uncertainty in electricity generation as these sources are intermittent and dependent on atmospheric conditions and spatial locations. Low predictability and variability of electricity generation from RESes can cause difficulties in sustaining a load-energy balance and/or power frequency in a grid, and thus can impose new challenges around power system reliability and stability. To continue utilizing these clean sources without endangering power system reliability, utilities implement various control mechanisms such as energy storage systems (ESSes), demand-side management (DSM), renewable energy curtailment (REC) and transmission switching (TS).

Energy storage systems are the most effective solutions for integrating RESes into the grid. These systems smooth the intermittency of RESes by storing electrical energy generated at off-peak hours to use at peak hours, and thus more electricity can be generated from RESes
and a substantial decrease in greenhouse gas emissions can be achieved.

Demand-side management is another control mechanism that helps utilities reduce demand at peak hours (referred to as load shedding (LS) in this paper) or reshape load profiles [3]. Efficient DSM can also reduce the need for peaking power plants and/or under-utilized electrical infrastructures, which can have high investment and operational costs. However, reducing demand at peak hours intentionally affects quality of life. Therefore, a penalty cost (value of lost load) is generally considered to compensate for the impact of cutting electricity [4].

Renewable energy curtailment is also used to handle RES variability. With an increase in RES penetration, a significant amount of renewable energy could be curtailed due to technical and operational reasons to maintain system voltage and frequency levels or to satisfy minimum generation requirements from thermal sources [5]. However, by lowering RES supply, the benefits of using clean sources and revenues from renewable generators are reduced. Thus, to promote new investments in sustainable energy, in some markets, revenue losses from renewable energy generators are sometimes compensated for in some contracts/policies [6,7].

Transmission switching is another control mechanism that adds flexibility to the grid. Transmission congestion, which is another reason for low RES shares in electricity generation, can be prevented by changing the status of transmission lines [8]. Thus, by applying TS operations (switching some lines out of service), RES penetration can be easily increased. Reducing congestion on transmission lines may also improve the efficiency of other components (e.g. generation units) or other control mechanisms, such as ESS, LS and REC. Making optimal siting and sizing decisions for ESS by considering TS operations can decrease the total investment cost of ESS. In addition, efficient DSM policies can be applied with the integration of TS, and thus LS, which is due to transmission congestion, can be minimized. Last but not least, as REC can be a significant waste, especially for countries that have renewable energy targets (such as Australia, Turkey, Brazil and Ireland [9,10]), TS can be a more efficient and cheaper solution compared to building new lines or more expensive ESSes. Therefore, considering TS in power system strategic and/or operational planning leads to higher social welfare by decreasing overall costs, enhancing quality of life and utilizing cleaner sources in electricity generation.

1.2. Literature review

Energy storage systems are effective solutions to the need for cleaner energy sources in electricity generation [4]. The value of ESSes has been increasingly discussed in the literature from different perspectives. Most studies focus on system operation and determine the ESS’ state of charge (SOC) for each time period [11]. In these studies, given the locations and sizes of the storage units, the aim is to maximize profit by bidding/selling operations in energy markets. However, these studies ignore the effect of ESS locations and sizes (e.g. [12]). To address this deficiency, other studies consider ESS locations and operations simultaneously for multi-stage [13], robust [14] and long-term [15] planning problems. There are also a few studies that optimize only ESS sizes under demand and generation uncertainties [16].

To fully reveal the benefits of ESSes, their siting and sizing decisions should be considered simultaneously during the planning stage; however, few papers focus on this co-optimization. Pandžić et al. [11] propose a three-stage heuristic algorithm to solve the co-optimized problem. Wogrin and Gayme [17] analyze ESS sizes for different technology types, such as pumped storage hydro, compressed-air energy storage, lithium ion batteries and fly-wheel energy storage, and conclude that the ESS sizes and locations are affected by technology type. Fernández-Blanco et al. [18] examine the effect of REC penalty costs and the capital costs of storage units on optimal ESS locations and sizes. Go et al. [19] assess the value of co-optimizing ESS, generation and transmission expansion planning on the IEEE 24-bus power system. They consider renewable portfolio standards and require a minimum generation from renewable sources. Xiong and Singh [20] limit the budget of ESS investments and discuss the effect of budget on ESS locations. Qiu et al. [21] focus on long-term planning and minimize total system cost considering battery lifetime and degradation.
The benefits of TS are discussed in many studies from perspectives such as reliability [22,23], economic efficiency [24] and expansion planning [25]. The beneficial impacts of TS on real-world examples are also discussed in [26] for the California and New England independent system operators (ISOs), and in [27,28] for the PJM system. However, only a few papers discuss the effect of TS on RES penetration. Villumsen et al. [29] analyze the effect of TS on wind power penetration levels and line capacity expansion plans. Qiu and Wang [30] discuss the effect of TS on total system cost and utilization of wind power, considering the uncertainty of wind power generation. Nikoobahkt et al. [31] develop a linearized AC model to analyze TS operations and RES utilization. However, none of these studies include ESSes. To the best of our knowledge, only a few papers simultaneously consider TS operations and ESS investment planning. Nikoobahkt et al. [32] and Aghaei et al. [33] optimize TS and storage operations in a unit commitment problem without allowing new investments. Dehghan and Amjadi [34] discuss an investment planning problem and determine the locations of new transmission lines and storages. However, these studies do not consider ESS sizing decisions.

In Table 1, we compare our study with the existing literature; except for our study, there is no paper that co-optimizes TS operations, transmission and ESS investments (i.e. ESS locations and sizes). A vertically integrated utility where a central planner makes all investment decisions become more prominent as the limits of new transmission lines and storages. However, these studies do not consider ESS sizing decisions.

In this section, we introduce our model, which jointly optimizes new investments and operational decisions. As the aim of this paper is to present the joint benefit of ESSes and TS, we assume that planning is done by a vertically integrated utility. For accurate representation of storage units, we consider both energy capacity and power ratings (ramp rates for charging/discharging) of ESSes. In our model, we ignore the cost for generating electricity from available RESes, as customarily done in the literature. For the sake of computational tractability, a static planning approach and a DC approximation of power flow constraints, as given in [35], are used in the proposed model, as also used in [15,19,34].

2. Mathematical model

In this section, we introduce our model, which jointly optimizes new investments and operational decisions. The decisions made in the first stage include investments of transmission lines and ESSes. The second stage involves recourse actions that are based on operational decisions such as power flows, generation amounts and transmission line status (open/closed) at each hour of the representative days. Each representative day is considered as a scenario with probability $\pi$, which is proportional to the occurrence of similar days based on random observations in the target year.

The objective function minimizes the total investment costs of new transmission lines ($z_{\text{line}}$) and storage units ($z_{\text{storage}}$), as well as the expected operational costs of conventional generators and ESSes ($z_{\text{op}}$).

The objective function is presented below and subject to the following constraints:

$$\min \quad z_{\text{line}} + z_{\text{storage}} + z_{\text{op}}$$

$$z_{\text{line}} = \sum_{a \in A, \ell \in E} c_{\text{line}}^a L_{a\ell}$$

$$z_{\text{storage}} = \sum_{r \in R} \left( c^r V^r + c^r F^r \right)$$

$$z_{\text{op}} = \sum_{e \in E} \sum_{L \in \mathbb{L}} c^e_{G_{\text{loss}}} \left( \sum_{a \in A, \ell \in E} c_{\text{line}}^a L_{a\ell} \right)$$

- Power Balance Constraint:
\[
\sum_{g \in C} G_{g_i} + \sum_{a \in A^{T}(a)} f_{a_i} - \sum_{a \in A^{T}(a)} f_{a_i} - P_{in}^d + P_{in}^d = D_{int} - DS_{int} \quad \forall \ i \\
\in B, \ t \in T, \ s \in S
\] (2)

Constraint (2) guarantees the power balance at node \( i \) at each time period, which includes generation from both conventional and renewable sources, incoming/outgoing flows, ESS charging and discharging rates and demand and load shedding amounts.

- **Generation Dispatch Constraints:**
  \[
  G_{g_i} \leq \mathcal{G}_{g_i} \quad \forall \ i \in B, \ g \in C, \ t \in T, \ s \in S
  \] (3)

- **Network Constraints:**
  \[
  G_{g_i} \leq G_{g_i} \leq G_{g_i} \quad \forall \ i \in B, \ g \in C \setminus C, \ t \in T, \ s \in S
  \] (4)

\[ R_{g} \leq G_{g_i} - R_{g} \leq R_{g} \quad \forall \ i \in B, \ g \in C \setminus C, \ t \in T, \ s \in S \] (5)

Constraints (3) and (4) set lower and upper bounds for electricity generation from renewable and conventional sources, respectively. Constraint (5) limits the maximum allowable change of generation from conventional sources between consecutive time periods.

- **ESS Constraints:**
  \[
  P_{in}^d \leq F(1 - X_{in}) \quad \forall \ i \in B, \ t \in T, \ s \in S
  \] (17)

\[ aY_{i}^d \leq Y_{i}^d \quad \forall \ i \in B, \ t \in T, \ s \in S \] (18)

\[ E_{in} = E_{in} + E_{in} Y_{i}^d \quad \forall \ i \in B, \ s \in S \] (19)

Constraint (10) satisfies the energy balance between consecutive time periods. Constraint (11) limits storage units SOC levels by their capacities, and Constraint (12) guarantees that storage capacity is between the predetermined lower and upper bounds. Constraint (13) also sets lower and upper bounds for storage units’ power ratings. Constraints (14) and (15) are the ramp rate of the storage units and limit their charging and discharging rates by their power ratings. Constraints (16) and (17) prevent ESSes from simultaneously charging and discharging [19]. Constraint (18) relates energy capacity and power rating via a given ratio. A daily storage cycling constraint (19) is added to enforce the storage energy balance for each representative day, as in [15,17,19].

- **LS and REC Constraints:**
  \[
  \sum_{i \in B} \sum_{i \in T} D_{in} \leq p^b \sum_{i \in B} \sum_{i \in T} D_{in} \quad \forall \ s \in S
  \] (20)

\[ \sum_{i \in B} \sum_{i \in T} \sum_{g \in g} \sum_{i \in T} G_{g_i} \geq (1 - P_{in}^e) \sum_{i \in B} \sum_{i \in T} \sum_{g \in g} \sum_{i \in T} G_{g_i} \quad \forall \ s \in S \] (21)

As explained earlier, instead of using monetary values for LS and REC, we limit their amounts. Constraints (20) and (21) set upper bounds for the LS and REC amounts, respectively.

- **Domain Constraints:**
  \[ L_{a} = 1 \quad \forall \ a \in EA \] (22)

\[ \delta_{off,a} = 0 \quad \forall \ t \in T, \ s \in S \] (23)

\[ -\pi \leq \delta_{in} \leq \pi \quad \forall \ i \in B, \ t \in T, \ s \in S \] (24)

\[ G_{g_i} \geq 0, \ \delta_{in} \geq 0 \quad \forall \ i \in B, \ g \in C, \ t \in T, \ s \in S \] (25)

\[ P_{in}^d \geq 0, \ P_{in}^d \geq 0, \ X_{in} \geq 0, \ E_{in} \geq 0, \ DS_{in} \geq 0 \quad \forall \ i \in B, \ t \in T, \ s \in S \] (26)

\[ L_{a} \in [0, 1], \ f_{in} \geq 0, \ Z_{in} \in [0, 1] \quad \forall \ a \in A, \ t \in T, \ s \in S \] (27)

\[ Y_{i} \in [0, 1], \ Y_{i}^d \geq 0, \ \forall i \in B \] (28)

Constraints (22)–(28) are for the domain restrictions of the decision variables. Constraint (22) is for the existing lines and Constraint (23) is the reference point for the buses’ voltage angles. The remaining constraints are the nonnegativity and binary constraints for the decision variables.

### 2.2. Linearization of the model

We note that the model is nonlinear due to the multiplication of decision variables in Constraint (7). Here, we linearize the model by utilizing the Big-M type of linearization technique. Two nonnegative flow variables, \( f_{a_i}^+ \) and \( f_{a_i}^- \), each one representing flow on the same line in one direction, express \( f_{a_i} \) as follows:
\[ f_{at}^+ = f_{at}^- - f_{at}^- \forall a \in A, \ t \in T, \ s \in S \]  
\[ \theta_{at} - \theta_{at}^- = \Delta \theta_{at}^+ - \Delta \theta_{at}^- \forall a \in AS_j, \ t \in T, \ s \in S \]

Similarly, two nonnegative variables, \( \Delta \theta_{at}^+ \) and \( \Delta \theta_{at}^- \), express the voltage angle difference between buses \( i \) and \( j \) as follows:

\[ f_{at}^+ \leq \varphi \Delta \theta_{at}^+ \forall a \in AS_j, \ t \in T, \ s \in S \]  
\[ f_{at}^- \leq \varphi \Delta \theta_{at}^- \forall a \in AS_j, \ t \in T, \ s \in S \]  
\[ f_{at}^+ \geq \varphi \Delta \theta_{at}^+ - M_{a} (1 - \text{Z}_{at}) \forall a \in AS_j, \ t \in T, \ s \in S \]  
\[ f_{at}^- \geq \varphi \Delta \theta_{at}^- - M_{a} (1 - \text{Z}_{at}) \forall a \in AS_j, \ t \in T, \ s \in S \]

Constraints (31)-(34) correctly linearize (7) for a sufficiently large positive number, \( M_a \), in Constraints (33) and (34). If line \( a \) is open (i.e. \( \text{Z}_{at} = 0 \)), Constraints (33) and (34) become redundant as \( f_{at}^+ \) and \( f_{at}^- \) are already larger than or equal to zero. For this case, Constraints (31) and (32) are also redundant, as \( f_{at}^- = 0 \) from Constraint (6). When \( \text{Z}_{at} = 1 \), Constraints (31) and (33) reduce to \( f_{at}^+ = \varphi \Delta \theta_{at}^+ \) and Constraints (32) and (34) reduce to \( f_{at}^- = \varphi \Delta \theta_{at}^- \). By using the equalities in (29) and (30), we obtain \( f_{at}^- = \varphi (\theta_{at}^- - \theta_{at}^-) \), which is the same equation obtained from Constraint (7) with \( \text{Z}_{at} = 1 \). Thus, adding constraints (29)-(34) and removing Constraint (7) linearizes the proposed model, and we obtain a mixed integer linear programming (MILP) model for the extensive form of the two-stage stochastic programming model given above.

In our model, we do not include features such as the start-up/shutdown status of conventional plants or the voltage angle differences of transmission lines after closing the lines. A model including these features leads to a problem that requires more computational power. In this paper, as our aim is to discuss the value of ESSes and TS, we limit our discussion to the detail given above.

3. Computational study

This section analyzes the benefits from co-optimizing transmission switching and other control mechanisms, such as energy storage systems, renewable energy curtailment and load shedding as a policy of demand-side management. The effect of TS on total system cost, LS and REC, as well as the locations and sizes of ESS are discussed in detail. The model is applied to the IEEE Reliability test system for varying limitations on LS and REC amounts.

3.1. Data

As shown in Fig. 1, the IEEE Reliability test system includes 24 buses, 32 generation plants located at 10 buses and 34 corridors for transmission lines. In the original network, the total installed capacity and total peak demand are 3405 MW and 2805 MW, respectively [36]. To induce congestion in the system and observe the value of TS in a power system with a high level of renewable energy penetration, we reduce the transmission line capacities by 50% and the installed capacity of thermal sources by 75%. Following [19], we allow wind and solar sources at six buses; solar generation units are available at buses 3, 5 and 7, and wind generation units are available at buses 16, 21 and 23. The installed capacities of new generation units, cost of transmission lines and ESS characteristics (e.g. round-trip efficiency, capital and discharging costs) are also obtained from [19]. We limit ESS capacity to 1000 MWh/bus, select an energy-power ratio of six hours and a round-trip efficiency of 81%. Annualized investment costs of energy capacity and power rating of ESS are $4000/MWh and $80,000/MW, respectively, and the discharging cost of ESS is $5/MW [19]. We also limit the installed capacity of solar and wind generation units to 1500 MW/bus and 1000 MW/bus, respectively.

![Fig. 1. Modified IEEE 24-bus power system.](image-url)
The duration of each time period is set to one hour. Hourly wind and solar profiles are obtained using wind speed and solar radiation values from [37] and hourly demand profiles are obtained from [36]. To observe the joint effect of TS and ESSes, different profiles are used for each wind and solar generation unit. Since load and generation profiles are independent from each other, we use a K-means algorithm to select five representative days. The profiles, which are the centers of the clusters (or the closest profile to the center), are selected as the representative days. Using the cardinality of each cluster (i.e. occurrence of the similar days), we determine the probabilities of the representative days.

3.2. Computational analysis

In this section, we first compare the results obtained from the model when neither ESSes nor TS is used (Base case) with the version that only includes ESSes (ESS case). We further analyze the results obtained from the ESS case with the model that includes both ESSes and TS (ESS-TS case) to observe the value of TS. For these analyses, instead of using penalty costs for LS and REC policies, we vary the limits for the maximum allowable LS and REC amounts. Starting from the instance where there are no restrictions on meeting demand ($p^l = 1$) and using RESes in generated electricity ($p^{rc} = 1$), we gradually relax these limits and report the minimum cost, locations and sizes of ESSes for each combination of $p^l$ and $p^{rc}$. Unless otherwise stated, in all experiments for the ESS-TS case, we limit the number of switchable lines to five and report the solutions with a 1% optimality gap. Experiments are implemented in Java platform using Cplex 12.7.1 on a Linux OS environment with Dual Intel Xeon E5-2690 v4 14 Core 2.6 GHz processors with 128 GB of RAM. The optimal solutions for the Base and ESS cases are obtained within five minutes and six hours, respectively. However, the solution times increase up to 35 h for the ESS-TS case, as the model optimizes TS operations and ESS siting and sizing simultaneously. We also note that in all three cases, solution times increase as $p^l$ and/or $p^{rc}$ decrease.

3.2.1. Effect of TS on the total system cost and value of ESSes

Fig. 2 shows the optimal costs of the three cases for different combinations of $p^l$ and $p^{rc}$. As we have the minimum generation requirement from conventional sources, in all cases the solutions obtained with the most relaxed instance, ($p^l$, $p^{rc}$) = (1.0, 1.0), is also equal to the solutions obtained with ($p^l$, $p^{rc}$) = (0.4, 0.5). Moreover, relaxing the limits only for $p^l$ or only for $p^{rc}$ beyond this point does not change the optimal solutions. Therefore, we ignore those regions and focus only on the solutions obtained with $p^l \leq 0.4$ and $p^{rc} \leq 0.5$. We first note that in all cases, reducing the ratios generally increases the optimal costs, as more investments are necessary to either meet the predetermined ratio of the total load or generate more electricity from RESes. However, guaranteeing the required generation from RESes needs more investments compared to the required investments for meeting the predetermined ratio of the load because the highest total system costs are obtained from the solutions with $p^{rc} \leq 0.2$.

Fig. 2 also presents the value of ESSes and the joint benefit of ESSes and TS in a power system with a high level of renewable energy penetration. For the Base case, we cannot obtain any feasible solutions for the instances with $p^l \leq 0.1$ or $p^{rc} \leq 0.4$ (Fig. 2a and Fig. 2d). However, by adding storage units to the same power system, we obtain solutions for these instances (Fig. 2b and Fig. 2e). Further, by also integrating TS, we find better solutions (Fig. 2c and Fig. 2f) than those obtained only with ESSes.

To observe the value of TS, we compare the optimal solutions of the ESS and ESS-TS cases. Table 2 presents the percentage improvements in total cost for different values of $p^l$ and $p^{rc}$ after incorporating TS operations, and Fig. 3 visualizes these improvements. Transmission switching decreases the total cost in all instances, and on the average, the saving is about 8.5%. Although the effect of TS is not significant for low $p^l$ or low $p^{rc}$ values, TS substantially reduces the total costs for the remaining $p^l$ (0.15 $\leq p^l \leq 0.4$) and medium $p^{rc}$ (0.3 $\leq p^{rc} \leq 0.4$) values. Therefore, if there are no TS operations, system operators must...
build new ESSes and/or lines and use more conventional power plants for electricity generation. However, by using TS operations, system operators require fewer investments to satisfy the same limits. Our results show that total cost can be reduced up to 16.27% when TS operations are incorporated into a power system.

According to the savings obtained by different $p^\text{ls}$ and $p^\text{rec}$ limits, it is possible to partition the results in Table 2 into four zones to observe the underlying reasons behind the shape presented in Fig. 3. For this analysis, we also detail the optimal solutions of the ESS and ESS-TS cases, and Fig. 4 demonstrates the differences between the objective functions of the two cases in monetary values, in terms of $z_{\text{line}}$, $z_{\text{stor}}$ and $z_{\text{trans}}$. When $p^\text{ls}$ is lower ($p^\text{ls} < 0.1$ (Zone A)), in response to the reduction in ESS investment costs and hourly operations, the same or more lines are required in the ESS-TS case, except for in one instance, where savings from using TS are limited due to increases in $z_{\text{line}}$. When $p^\text{ls}$ is higher ($p^\text{ls} \geq 0.2$) and $p^\text{rec} \leq 0.25$ (Zone B), TS decreases the optimal value of $z_{\text{line}}$ and/or $z_{\text{stor}}$. However, savings from TS are also limited because investments for lines and for ESSes are needed in the ESS-TS case in order to meet the generation requirement. For these instances, we also observe that electricity generation from conventional sources are at their minimum levels in both cases.

When both $p^\text{ls}$ and $p^\text{rec}$ are high (i.e. $p^\text{ls} \geq 0.2$ and $p^\text{rec} \geq 0.45$ (Zone D)), there is no need in either case to build new lines. Thus, TS decreases only the operational and storage investment costs in most instances. We also note that the improvements in the last column of Table 2 are only due to savings from operational costs because neither ESSes nor transmission lines are built for these cases. In our experiment setting, the highest improvements are obtained when $p^\text{ls} \geq 0.2$ and $0.3 \leq p^\text{rec} \leq 0.4$ (Zone C). Although the decreases in operational costs are small, the required investment costs of transmission lines and/or ESSes are significantly reduced. We refer to instances with $p^\text{ls} = 0.15$ as transition zones because some of the solutions are similar to the solutions in Zone A and some of them are similar to the solutions in Zones B, C or D.

We also analyze the solutions in each row in Zones B through D. Transmission switching operations first yield to savings from ESS investment costs and then transmission line investment costs. Further relaxing the renewable generation requirement, increases the savings in both assets, as in Zone C. Passing from Zone C to Zone D decreases savings from the assets because transmission lines and ESSes are not needed in the ESS or ESS-TS case. However, in Zone D, decreases in

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<th>$p^\text{rec}$</th>
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<th>0.30</th>
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Fig. 3. Visual representation of the effect of TS on the total system cost (%).

Fig. 4. Cost difference in the objective function components for the ESS case and the ESS-TS case.
operational costs become significant. We also note that we do not obtain smooth transitions or trends within or between the zones mainly due to the discrete sets that we have for \( p^\phi \) and \( p^{rec} \) values as well as the capacity of system components.

### 3.2.2. Effect of TS on siting and sizing of ESSes

As observed earlier, changing transmission line status decreases the total system cost, and one of the potential reasons for this decrease is because other components in the system are being used more efficiently. Therefore, TS operations can affect the number, sizes (i.e., energy capacity and power rating) and locations of storage units.

To observe the value of TS on ESS decisions, we compare the optimal results obtained with the ESS and ESS-TS cases. Table 3 presents the number of storage units, and they generally increase for both cases as we tighten \( p^\phi \) and \( p^{rec} \) limits. We also observe that the number of storage units are highly dependent on \( p^{rec} \) values. Although varying only \( p^\phi \) for any \( p^{rec} \) value does not change the number of ESSes in many instances, varying only \( p^{rec} \) for any \( p^\phi \geq 0.2 \) changes the number of ESSes from 11 to 0. Therefore, depending on system operators’ renewable energy targets, ESSes can play an important role.

Our results also demonstrate that increasing the efficiency of the system with TS operations generally leads to fewer storage units needed for the same limits. We also note that ESS locations are similar in both cases, and that ESSes are generally located close to renewable generation units or large conventional power plants (Fig. 1) to add flexibility to the grid to use the stored energy as required. More details about ESS locations can be found in Appendix Figs. 12-15.

Table 4 presents the improvements in the total energy capacity and power rating of ESSes when TS operations are used in the power system. The value of TS is significant for instances when \( p^\phi \geq 0.1 \) and \( 0.35 \leq p^{rec} \leq 0.4 \); up to 50.69% improvement on the total energy capacity and 57.52% improvement on the total power rating are obtained. As discussed above, improvements decrease when \( p^\phi \) or \( p^{rec} \) is low because investments are required in the ESS-TS case. Moreover, in five instances, when \( p^{rec} \) is equal to 0.45, the storage units built in the ESS case are not needed in the ESS-TS case. Thus, 100% improvement is obtained in these instances. Details on the energy capacity and power rating of ESSes can be found in Appendix Figs. 12-15.

We now detail the locations and sizes of storage units for the highlighted row and columns in Table 4. In the following tables and figures, the row and the column are represented by \( (p^\phi, p^{rec}) = (0.2, :) \) and \( (p^\phi, p^{rec}) = (:, 0.4) \), respectively. Figs. 5 and 6 demonstrate the total energy capacity and power rating of storage units for the ESS and ESS-TS cases with \( (p^\phi, p^{rec}) = (0.2,) \) and \( (p^\phi, p^{rec}) = (:, 0.4) \), respectively. When we relax RES generation requirements (or increase \( p^{rec} \)) for the instances with \( p^\phi = 0.2 \) (Fig. 5), the total energy capacity and power rating of ESSes gradually decrease in both cases. On the other hand, relaxing \( p^\phi \) up to 0.15, for the instances with \( p^{rec} = 0.4 \) (Fig. 6), significantly reduces the energy capacity and power rating in both cases. Thus, while we conclude that energy storage is a very effective component of the system for meeting the various \( p^{rec} \) limits, the role of storage is limited to only very small \( p^\phi \) values, and the effect of TS on this role of the storage becomes more prominent as the constraints on RES and LS are relaxed.

For the results obtained with \( (p^\phi, p^{rec}) = (0.2,) \) and \( (p^\phi, p^{rec}) = (:, 0.4) \), Figs. 7-10 detail the results of ESS by presenting the changes in their locations and sizes when TS is incorporated into the power system. In the figures, we only focus on the differences, and do not include storage units built at the same bus with the maximum allowable energy capacity or power rating in the ESS and ESS-TS cases. One can find the storage units with the maximum sizes in both cases in Appendix Tables 5 and 6. So far, we have presented that TS can decrease the total number of storage units (Table 3) and/or the total energy capacity and power rating (Table 4). These conclusions can also be observed in Figs. 7-10. For example, in the solution obtained with \( (p^\phi, p^{rec}) = (0.15, 0.4) \), in both the ESS and ESS-TS cases, the size of the storage units located at buses 5 and 21 are almost the same. In the ESS-TS case, by not needing to build the storage at bus 7 that is located in the ESS case, the number of storage units in the system decreases by one. Even when the number and locations of storage units are the same, TS can decrease the total storage size, as in \( (p^\phi, p^{rec}) = (0.2, 0.35) \).

Transmission switching can also affect the locations of storage units

---

Table 3

<table>
<thead>
<tr>
<th>ESS case</th>
<th>ESS-TS case</th>
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<tr>
<td>( p^{rec} )</td>
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<tr>
<td>( p^\phi )</td>
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Table 4

<table>
<thead>
<tr>
<th>Improvements in ESS sizes due to TS (%)</th>
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</thead>
<tbody>
<tr>
<td>( p^{rec} )</td>
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<tr>
<td>( p^\phi )</td>
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</tr>
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<td>0.05</td>
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<tr>
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<td>0.15</td>
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<tr>
<td>( p^\phi )</td>
</tr>
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in the system. For instance, as in the solution obtained with 
\((p^i, p^{rec}) = (0.1, 0.4)\), in the ESS-TS case, new storage 
is built at bus 22 instead of at bus 2 in the ESS case. Therefore, not only for short-term 
operational decisions, but also for medium- to long-term planning de-
cisions, as discussed in [34] without considering ESS sizing, the e 

effect of TS can be significant depending on load targets and/or RES utilization 
levels.

3.2.3. Effect of TS on REC and LS

Previous sections discuss the effect of TS on the total system cost 
and on ESS locations and sizes. We show that TS adds flexibility to the 
grid, increases component efficiency and generates more electricity 
from RESes to meet demand. Therefore, in addition to reducing the 
total system cost and storage sizes, TS inherently increases the share of 
RESes in the total supply.

Although the benefit of TS on REC is obvious in some instances, 
such as \((p^i, p^{rec}) = (0.2, 0.5)\), where the total system cost decreases due 
to an increase in generation from RESes, the benefit of TS on LS is not 
obvious due to the discretization of \(p^i\) and \(p^{rec}\). In order to handle this 
deficiency and examine the effect of TS on LS, we modify the proposed 
model from Section 2. We provide the following multi-objective 
mathematical programming model that minimizes \(p^i\) and \(p^{rec}\) as two 

\[
\min \quad p^i 
\] (35)
\[
\begin{align*}
\min & \quad p^{\text{rec}} \\
\text{s.t.} & \quad \sum_{i \in B} \sum_{e \in T} D_{\text{dis}} \leq p^\text{in} \sum_{i \in B} \sum_{e \in T} D_{\text{in}} \quad \forall s \in S \\
& \quad \sum \sum G_{ij} \geq (1-p^{\text{rec}}) \sum \sum C_{ijs} \quad \forall s \in S \\
& \quad z_{\text{line}} + z_{\text{storage}} + z_{\text{om}} \leq \text{budget} \\
& \quad (2) - (5), (8) - (28)
\end{align*}
\]
In the model presented above, \( p^0 \) and \( p^{\text{rec}} \) are the decision variables and Constraints (20) and (21) determine the minimum \( p^0 \) and \( p^{\text{rec}} \) in the system, respectively. For this analysis, we also limit the total system cost with a budget represented by Constraint (37).

The \( \varepsilon \)-constraint method is a widely used approach for solving multi-objective problems [38]. In this method, one of the objective functions is selected to be optimized and the other one is added to the model as a new constraint with a bound. In this study, a variation of this method is used to obtain only non-dominated solutions. In the augmented \( \varepsilon \)-constraint method [38], the second objective is also added to the objective function by multiplying with a small coefficient, \( \gamma \). By sequentially increasing/decreasing the bound of the second objective, \( \varepsilon \), all Pareto-optimal solutions are found. The objective function and the new constraint added to the model to solve the problem with the \( \varepsilon \)-constraint method is represented as follows:

\[
\min \ p^0 + \gamma p^{\text{rec}} \quad (38)
\]

\[
p^{\text{rec}} \leq \varepsilon \quad (39)
\]

For discussing the effect of TS on REC and LS, we utilize the solution obtained with \((p^0, p^{\text{rec}}) = (0.2, 0.4)\) for the ESS case and limit the total system cost by $148,741 M, which is the optimal solution value of that instance.

Fig. 11 demonstrates the sets of pareto optimal solutions for the ESS and ESS-TS cases. Transmission switching operations improve the efficiency of the power system and yield to lower \( p^{\text{rec}} \) limits for the same \( p^0 \). Moreover, TS operations decrease the minimum \( p^0 \) limit from 0.18 to 0.16. We also emphasize that the highest RES penetration level, (i.e. the lowest \( p^{\text{rec}} \)) in the ESS case (37.71%) is worse than the lowest RES penetration level, (i.e the highest \( p^{\text{rec}} \)) in the ESS-TS case (37.75%). Hence, TS helps system operators increase the share of RES in the total supply and improve quality of life without allocating more resources. We note that these results are clearly dependent on a predetermined budget, and therefore, the value of TS could be more significant with budget limits other than the one presented here.

### 4. Conclusion

This paper provides a mathematical model that co-optimizes transmission switching operations, ESS siting and sizing decisions and considering limits on maximum allowable load shedding and renewable energy curtailment amounts in the power system. Utilizing an extensive computational study on the IEEE 24-bus power system, we precisely characterize the effect of transmission switching on total system cost, ESS locations and sizes, load shedding and renewable energy curtailment control mechanisms. Our results provide insights about the role of storage at different limits for load shedding and renewable energy curtailment control mechanisms; the modeling framework discussed in this study can also be extended to optimizing storage portfolios for power systems. Our results show that total system cost and total ESS size can be decreased up to 17% and 50%, respectively, and the full potential of ESS in the power system can be revealed for a vertically integrated utility when switching operations are utilized. The results also demonstrate that switching lines helps system operators use their budgets to apply better demand-side management and/or renewable energy curtailment policies due to increased utilization of system components.

In this paper, we present a static planning model to constitute a balance between computational complexity and solution quality. However, this model can easily be adapted to the dynamic planning problem, where (with increased solution time) the time of building new transmission lines and storage units can be determined. Moreover, incorporating features such as start-up and shut-down status of conventional plants leads to a problem with more computational complexity. Thus, good heuristics and/or sophisticated solution techniques could be future research directions to explore applying this problem to larger and real-world power systems.

### Appendix A

Tables 5 and 6

### Table 5

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<th>( p^{\text{rec}} )</th>
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Table 6
ESS locations with maximum power rating common to the ESS and ESS-TS cases.

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Figs. 12–15

![Graph showing ESS locations and energy capacities (MWh) for the ESS case.](image-url)
Fig. 13. ESS locations and energy capacities (MWh) for the ESS-TS case.
Fig. 14. ESS locations and power ratings (MW) for the ESS case.
References


