Elucidating the Barriers on Direct Water Splitting: Key Role of Oxygen Vacancy Density and Coordination over PbTiO$_3$ and TiO$_2$

Ersen Mete,* Şinasi Ellialtıoğlu, Öguz Gülseren, and Deniz Uner*

ABSTRACT: In this work, using the state-of-the-art first-principles calculations based on density functional theory, we found that the concentration and coordination of surface oxygen vacancies with respect to each other were critical for the direct water-splitting reaction on the (001) surfaces of PbTiO$_3$ and TiO$_2$. For the water-splitting reaction to happen on TiO$_2$-terminated surfaces, it is necessary to have two neighboring O vacancies acting as active sites that host two adsorbing water molecules. However, eventual dissociation of O$^-$H bonds is possible only in the presence of an additional nearest-neighbor O vacancy. Unfortunately, this necessary third vacancy inhibits the formation of molecular hydrogen by trapping the dissociated H atoms on TiO$_2$-terminated surfaces. Formation of up to three O vacancies is energetically less costly on both terminations of PbTiO$_3$(001) surfaces compared with those on TiO$_2$; the presence of Pb leads to weaker O bonds over these surfaces. Molecular hydrogen formation is more favorable on the PbO-terminated surface of PbTiO$_3$, requiring only two neighboring oxygen vacancies. However, the hydrogen molecule is retained near the surface by weak van der Waals forces. Our study indicates two barriers leading to low productivity of direct water-splitting processes. First and foremost, there is an entropic barrier imposed by the requirement of at least two nearest-neighbor O vacancies, sterically hindering the process. Furthermore, there are also enthalpic barriers of formation on TiO$_2$-terminated surfaces or removal of H$_2$ molecules from the PbO-terminated surface. The requirement dictating three nearest-neighbor oxygen vacancies for hydrogen evolution is also consistent with the chemical intuition: The nearest neighbor of the formed hydrogen should be reduced enough to inhibit spontaneous oxidation under ambient conditions.

1. INTRODUCTION

Understanding and finding a route toward an efficient water-splitting reaction is not only important for energy and technological applications but also essential from the fundamental point of view. Several different model systems like titania or perovskite surfaces have been proposed and investigated for this purpose. Existing routes for hydrogen production from renewable energy include (i) using renewable electricity for electrolysis of water, (ii) using concentrated solar energy for steam and/or carbon dioxide reforming of methane, and (iii) photoassisted catalytic or electrochemical water splitting. If proven successful, photo(electro)-chemical production of hydrogen is the most attractive due to the simplicity of the process and the potential this simple process offers. Both direct photo-electrochemical and photocatalytic water splitting suffer from two problems. The first problem is the low production rates and photon conversion efficiencies. The second problem, which is also directly related to the first problem, is the difficulty with which the structures release oxygen for a complete catalytic cycle. In photo-electrochemical processes, the bottleneck is the oxygen release. The thermodynamic driving forces under ambient conditions are toward water; hence, once hydrogen and oxygen molecules are produced, their contact must be avoided to inhibit spontaneous combustion. This condition is present in electrochemical cells in which the anode and cathode are connected through a circuit and an electrolyte, but the produced hydrogen and oxygen are collected separately. Still, in the electrochemical systems, the bottleneck is the oxygen evolution reaction. The current consensus for the prevailing mechanism of oxygen evolution in oxides or perovskites is through the formation of oxygen vacancy. The subsequent steps of this process depend on several factors including the nature of the oxide material.
On the contrary, photocatalytic hydrogen production is carried out in slurry-type suspended solid catalysts in solvents. Well-mixed conditions, needed for an efficient reaction, also provide the environment for the immediate back oxidation of hydrogen to water. These processes can be inhibited by a careful design of the photoreactor or designing catalysts where oxygen evolution and hydrogen evolution are delegated to different facets of the same crystallite. Despite the efforts, hydrogen production rates are within a few mmol/(h·g) catalyst as revealed by a thorough review of the literature, accompanied by the machine learning approaches.

The dilemma in all of these processes resides in the thermochemical bulk properties of the semiconductor oxides. The inherent photocatalytic activity of the semiconductor oxides depends on the capacity of bond breaking by the interaction of the oxide with electromagnetic radiation. The absorption of the electromagnetic radiation with the proper wavelength results in the creation of $e^-\cdot h^+$ pairs. The chemical nature of these $e^-\cdot h^+$ pairs depends on the oxide itself. For TiO$_2$, as an example, upon irradiation, $e^-$ finds a place on the Ti atom, changing the oxidation state from +4 to +3, while the bond between the oxygen and Ti atoms are broken. In other words, “softness” of the bonds between oxygen and metal atoms is required for photon absorption, and, on the other hand, softness is the reason that the formed hydrogen can interact with these bonds for oxidation. The chemical potential of the hydrogen formed is sufficient to reduce the lattice oxygen.

One final barrier in the efficient production of hydrogen is to remove the hydrogen formed by water splitting that is accommodated on the solid. Hydrogen can be accommodated in the form of spilled over hydrogen, which can be held around the surface or in the bulk. The limitations can also be due to kinetic metastabilities dictated by a low surface coverage of hydrogen atoms. The spatial separation may inhibit the formation of dihydrogen for desorption, hence lowering the productivity.

The objective of this study is to search the limits of the water-splitting reaction over TiO$_2$ and PbTiO$_3$ through first-principles methods. We determined the barriers to the formation and removal of molecular hydrogen on titania and lead titanate. We started our analysis by assuming that oxygen vacancies are available, acting as two neighboring active sites hosting two water molecules. We examined the possibility of water dissociation depending on the coordination and clustering of surface O vacancies by ab initio methods.

2. METHODS

Density functional theory (DFT) calculations were performed using VASP within the framework of the projector augmented-wave (PAW) method based on plane-wave expansion of single-particle states up to an energy cutoff value of 400 eV. The exchange and correlation effects were taken into account in the calculations by the SCAN (strongly constrained and appropriately normed) meta-GGA (semilocal meta-generalized gradient approximation) density functional. The SCAN functional lifts the overbinding in oxide materials, which is common to GGA functionals. The shortcoming of semilocal XC functionals in describing the electronic structures of materials associated with self-interaction (SI) can be overcome by either admixing the Hartree–Fock exchange with local density approximation (LDA)-based exchange terms or supplementing on-site Coulomb interaction for localized electrons, a method known as LDA + U. In particular, the transition-metal oxides with partially occupied d-states were erroneously predicted to be metallic by semilocal XC functionals. A proper description of both defect-related gap states and the band gaps can be obtained by imposing a suitably chosen $U$ parameter for Ti 3d states. Recently, the use of $U$ parametrization for O 2p states in oxides was shown to enhance the energetics and forces to match those of hybrid functionals. A systematic trace of the $U$-parameter space showed that defect-related electronic properties can be properly described when the SCAN functional is supplemented with parameters of $U = 6$ for Ti 3d and $U = 3$ for O 2p states. The calculated electronic band gaps of pristine PbTiO$_3$ and TiO$_2$ are 2.53 eV (exp. 2.5 eV) and 2.77 eV (exp. 3.1 eV), respectively. A 4 × 8 × 1 k-point mesh was used for Brillouin zone integrations. Atomic coordinates were fully relaxed by imposing a convergence criterion of $10^{-2}$ eV/atom for the minimization of Hellmann–Feynman forces on each atom in every spatial cartesian direction.

Both PbO and TiO$_2$ terminations of PbTiO$_3$-(001) (3 × 2) and TiO$_2$-(001) (3 × 2) surfaces were modeled as slabs that were constructed from their bulk phases, including 11 atomic layers along the [001] direction, to ensure the convergence of surface energies, as suggested previously. A vacuum region with a thickness of 12 Å along the surface normal was introduced in the computational supercells to avoid any unphysical interaction between the periodic images of the slabs. Full-geometry optimizations were performed without freezing any of the atoms to their bulk positions and without imposing symmetry. In addition, the postprocessing of the calculated data was needed to determine the charge accumulation around each atom, which was carried out using the Bader algorithm.

3. RESULTS AND DISCUSSION

There are basically two possible terminations for the lowest index (001) plane of PbTiO$_3$. These are the PbO and TiO$_2$ surface layers. The latter has the lowest surface energy among all possible cleavages including higher-index planes. Therefore, the (001) surface with TiO$_2$-termination is the most stable surface of PbTiO$_3$. When there are oxygen deficiencies on the surface, TiO$_2$-termination energetically becomes even more favorable than the PbO termination.

Water-splitting reactions, whether thermochemical, electrochemical, or photocatalytic, involve reduction of oxide materials through an energy source such as heat, electrons, or photons. Therefore, oxygen vacancies play an important role in capturing and splitting of water molecules. We explored the necessary requirements for the direct splitting of water molecules via surface oxygen vacancies on PbTiO$_3$ and TiO$_2$. The conditions depend not only on the material but also on the termination due to different surface chemical reactivities.

The TiO$_2$-terminated top layer of PbTiO$_3$ mimics titania surfaces and provides a setting for a variety of chemical reactions. For instance, molecular adsorbates tend to exhibit similar adsorption characteristics to those on the anatase (001) surface. Bonds usually form between their tail oxygens and surface Ti atoms. This looks like a continuation of the bulklike TiO$_2$ structure. In an experimental realization, the surface might have oxygen vacancies that leave excess charge around the nearest-neighbor Ti atoms. Such vacancy sites become
more active in capturing molecules, leading to relatively stronger binding.

The energy required to remove an oxygen atom from the surface is 3.86 eV on the PbO-terminated and 3.96 eV on TiO2-terminated surface. It is energetically 0.1 eV more favorable on the PbO-terminated surface. The formation energy of an oxygen vacancy on the surface of titania is 4.39 eV (Table 1). We explored necessary conditions for hydrogen molecule formation as a result of oxygen vacancy-induced splitting of water on the surfaces. To examine the possibility of splitting two adjacent water molecule adsorbates into their hydrogen atoms and hydroxyl groups on the surfaces, we considered a number of configurations. As a starting point, the minimum condition appears to be the availability of adjacent surface oxygen vacancies that act as an adsorption center. The adsorption of two water molecules at the two adjacent oxygen vacancy sites allows close proximity for the nearest-neighbor hydrogen atoms that face each other in the lateral direction.

The energy cost of formation of two and three neighboring surface oxygen vacancies, in Table 1, increases depending on the material and surface termination; the formation energy per vacancy appears to slightly fluctuate around the value of a single vacancy.

In the case of TiO2 termination on both titania and lead titanate, the adsorption geometry of two water molecules at the two neighboring oxygen vacancy sites is shown in Figures 1b and 2b, respectively. Formation of Ti−O bonds as a result of charge transfer from the surface Ti to oxygen atom due to water adsorption leads to weakening of O−H bonds within the water molecule. Bader analysis, as a comparison of the total charge on the substrate before and after adsorption, shows a charge transfer of 1.43 and 1.39 electrons from the titania and TiO2-terminated lead titanate slabs, respectively. This type of surface oxidation and atomic configuration solely is not enough to achieve water splitting. The DFT calculations indicated that there is a need for an additional oxygen vacancy that must also be adjacent to both of the adsorption sites, as shown in Figures 1b and 2b. Adsorption of water on the surface loosens the O−H bonds. Moreover, the water molecules slightly lean toward each other due to the presence of lateral Ti−O bonds between them. Then, the distance between the H atoms facing each other becomes as small as 1.8 Å in the lateral direction due to the presence of the third oxygen vacancy. This site has to remain as a vacancy to ensure breaking the O−H bonds. This mechanistic picture gives rise to the dissociation of H atoms from their parent water molecules, leaving the hydroxyl groups behind. The ratio of the clustering vacancies to the number of surface oxygens is 1/3. When we considered a cluster of four neighboring surface oxygen vacancies, the geometry optimization resulted in a significant local distortion, which drives the reduced surface layer to undergo reconstruction. These kinds of defect-driven structural changes due to oxygen vacancies are known for the formation of black TiO2.

Although the H atoms that were dissociated from their parent water molecules are close to each other, they did not form a H2 molecule. On TiO2 termination, these hydrogen atoms were, however, attracted to the adjacent oxygen vacancy sites, forming different adsorption geometries for titania and lead titanate due to differences in their chemical environment at the subsurface layers, as shown in Figures 1c and 2c. One of the main differences is the undulation geometry of the TiO2 network of the top layer, which mechanistically plays an important role in the subsequent pathway of the dissociated H atoms. The Ti−Ti separations on the surface layer are 3.79 and 3.89 Å on TiO2(001) and PbTiO3(001), respectively. Energetically, the adsorption of a water molecule at a surface oxygen vacancy site is considerably stronger on titania. The calculated adsorption energies are −1.43 and −1.11 eV on TiO2(001) and TiO2-terminated PbTiO3(001), respectively. On the surface of titania, both of the H atoms were trapped at the vacancy site, reflecting a Ti−H bonding character, as shown in Figure 1c. Bader charge analysis shows an accumulation of 1.66 electrons around this H atom, indicating partial filling of the 2s orbital. In this geometry, the position of lower-lying H mimics surface-like oxygen coordination with the nearest-neighbor Ti atoms. On the surface of lead titanate, one of the H atoms is attracted to the oxygen vacancy, while the other H atom is weakly bound atop the nearest-neighbor surface Ti atom (Figure 2c). Bader charges are 1.66 and 1.58 electrons for these H atoms, respectively. Both H atoms were trapped on the surface layer, preventing the formation of H2. Then, breaking of the translational symmetry induced by these impurities on the

**Table 1. Formation Energies (in eV) of Nearest-Neighbor Surface Oxygen Vacancies Calculated Using the SCAN XC Functional**

<table>
<thead>
<tr>
<th>surface model</th>
<th>1Ovac</th>
<th>2Ovac</th>
<th>3Ovac</th>
</tr>
</thead>
<tbody>
<tr>
<td>TiO2(001)-(3 × 2)</td>
<td>4.39</td>
<td>9.77</td>
<td>15.39</td>
</tr>
<tr>
<td>PbTiO3(001)-(3 × 2) TiO2-terminated</td>
<td>3.96</td>
<td>7.39</td>
<td>11.49</td>
</tr>
<tr>
<td>PbTiO3(001)-(3 × 2) PbO-terminated</td>
<td>3.86</td>
<td>8.12</td>
<td>11.37</td>
</tr>
</tbody>
</table>

Figure 1. Schematics of TiO2(001)-(3 × 2) (a) with a cluster of three adjacent oxygen vacancies (Ovac) only and (b, c) with additional two H2O adsorbates at the neighboring oxygen vacancy sites in their corresponding initial and final geometries, respectively. Light blue (Ti), red (O), and white (H) colors are used for the ball-and-stick illustration of the model structure.
surface layer influences the sublayer such that Pb atoms are distorted from their bulklike centoidal positions.

In the case of the PbO-terminated surface of PbTiO₃, when two water molecules are adsorbed on two nearest-neighbor oxygen vacancy sites, as shown in Figure 3b, they slightly lean toward each other and the O−H bonds loosen as a result of charge transfer from the substrate to the adsorbate; Bader analysis gave a value of 0.85 electrons for lead titanate. Then, the H−H distance becomes 1.8 Å similar to the previous cases. The adsorption energy per water molecule at a surface oxygen vacancy site is −0.97 eV, which is significantly lower in magnitude than those of TiO₂ terminations. Another important difference of PbO termination from the TiO₂ terminations is the coordination in the corresponding surface layers. The Pb−O bonds are 2.54 Å on PbO termination, while Ti−O bonds are 2.02 Å on TiO₂ termination. This indicates stronger coordination in the TiO₂ network. These factors can be attributed to the dissociation of H atoms from their parent water molecules because of the attraction between the two hydrogen atoms in close proximity to each other. They form a H₂ molecule, leaving the hydroxyl groups at the vacancy sites, because the required charge compensation is supplied by the Ti atoms that are exposed at the adsorption site. Bader charge analysis showed that the charge on each H atom that contributes to the covalent bonding in the hydrogen molecule is one electron, while the charge on the H atom of the hydroxyl group is zero. Then, the hydrogen molecule stays above the surface plane at a van der Waals distance (2.90 Å) due to the absence of an additional surface oxygen vacancy near the adsorption site, as shown in Figure 3c.

The energy level diagram for the pathway of water adsorption and dissociation on the oxygen-deficient surfaces is shown in Figure 4. Consistent with the calculated adsorption energies, the first stage from (a) to (b) describes the separate adsorption of two water molecules on two nearest-neighbor oxygen vacancies. Binding of water on TiO₂ is significantly stronger, which indicates the weakening of the lateral Ti−O bonds associated with Pb atoms in the case of PbTiO₃. Pb suppresses the undulation of the Ti−O layer. The lateral Ti−O bonds are 1.94 and 1.99 Å in titania and lead titinate, respectively. For the second stage from (b) to (c), TiO₂-terminated surfaces appear to be energetically more favorable for water splitting. We note that dissociation of water did not take place on TiO₂ terminations without an additional oxygen vacancy that connects the water adsorption sites. Therefore, at least a cluster of three oxygen vacancies is necessary on TiO₂ terminations. However, dissociation of water did not end up...
with H₂ production on the (001) surfaces of neither TiO₂ nor TiO₂-terminated PbTiO₃ for the oxygen vacancy-mediated models considered here. The energy differences from (b) to (c) are −3.12 eV (PbO termination of PbTiO₃), −2.13 eV (TiO₂ termination of PbTiO₃), and −3.51 eV (TiO₂). The only case that can produce H₂ appears to be PbO termination with two adjacent oxygen vacancies that were occupied with two separate water molecules even though the energy difference in the last stage is smaller than the other cases.

Total charge distributions, the energy bands, and the corresponding partial densities of states (PDOS) were calculated, as shown in Figure 5. Charge density plots show the bonding characteristics of TiO₂ and PbTiO₃ lattice structures. The calculated Bader charges are consistent with the nominal charge states for the lattice cations and anions as Ti⁴⁺, O²⁻, and Pb¹⁺. More importantly, the charge distribution after water dissociation reveals the bonding of dissociated H atoms to either the substrate or to each other to form H₂. Especially, the charge around the H atoms, which were bound to surface Ti atoms, indicates a partial filling of the 2s orbitals.

Energy bands and electronic densities of states were calculated using the SCAN functional with the supplementary Hubbard-U term to better describe the repulsion between strongly correlated Ti 3d and, to a lesser degree, O 2p electrons. This is one of the methods necessary to overcome the band gap underestimation of the standard XC functionals within the framework of DFT. After testing several U parameters for Ti 3d with and without O 2p orbitals, the optimal choice was found as U = 6 for Ti 3d and U = 3 for O 2p states, which not only heals the band gap but also gives a sound description of the defect-related gap states for both of the materials (please see the Supporting Information). In particular, the application of Hubbard-U for O 2p orbitals becomes important for the electronic description of dissociated H atoms on a cluster of three oxygen vacancies on TiO₂ termination of PbTiO₃.

The valence band (VB) dominantly reflects the Ti−O bonding character with a contribution from Pb−O bonds in the case of PbTiO₃. The upper part of VB is characterized by O 2p electrons, which is common and well known for transition-metal oxides. The conduction band (CB), on the other hand, dominantly contributed by antibonding Ti 3d states. In the cases of TiO₂-terminated surfaces shown in Figure 5a,b, two hydroxyls are bound to two adjacent vacancies. This binding appears as a doubly degenerate state reflecting Ti−O bonding character. In addition, trapping of dissociated H atoms at the third oxygen vacancy brings a flat going occupied state 0.73 and 0.55 eV below the conduction band minimum (CBM) of TiO₂ and PbTiO₃, respectively. Well localization of these defect-related states indicates a weak binding of dissociated H atoms to the vacancy site on the substrate. In the case of PbO termination of PbTiO₃ shown in Figure 5c, the valence band maximum (VBM) is characterized by the hydroxyl−vacancy bond similar to the previous structures. A gap state 0.34 eV [Γ−M] below the CBM appears due to H₂. The dispersion of this state along kₓ is consistent with the H−H covalent bond, which lies in the z-direction (or [001]) with respect to the surface plane. The SCAN + U method successfully explains and gives insights into
the origin and nature of the electronic energy band structure of the models, which were constructed to represent water splitting on TiO$_2$ and PbTiO$_3$.

4. CONCLUSIONS

The number and clustering of surface oxygen vacancies become critically important for direct water splitting on the (001) surfaces of TiO$_2$ and PbTiO$_3$. The presence of Pb weakens the binding of lattice oxygens. Therefore, the energy cost of oxygen vacancy formation on TiO$_2$ is higher than that on PbTiO$_3$. The minimum requirement appears to be the adsorption of two water molecules on two nearest-neighbor oxygen vacancy sites separately for the possibility of a subsequent dissociation of their H atoms that face each other. TiO$_2$-terminated surfaces need a cluster of three oxygen vacancies in which two of them act as water-capturing active sites and the remaining one must be adjacent to both of them and must remain unoccupied. The existence of this third vacancy is necessary for the dissociation of the H atoms from their parent water molecules yet is detrimental for the formation of H$_2$ since it acts as a trap for dissociated H atoms. Revelation of this bottleneck is useful in explaining the production of very low quantities of H$_2$ by direct water splitting on TiO$_2$ terminations, which are otherwise known for their excellent catalytic properties. On PbO termination of PbTiO$_3$, two adjacent oxygen vacancies can capture two water molecules that lean toward each other. Based on the DFT calculations, vacancy-mediated water splitting seems to be possible on PbO termination. However, hydrogen molecules must overcome the van der Waals attraction toward the surface.

■ ASSOCIATED CONTENT

Supporting Information
The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcc.0c09685. 3D charge density plots and energy band structures calculated using different $U$ parameters for the (001) terminations of PbTiO$_3$ and TiO$_2$ (PDF)

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Supporting Information

Elucidating the Barriers on Direct Water Splitting: Key Role of Oxygen Vacancy Density and Coordination over PbTiO$_3$ and TiO$_2$

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1. Dissociation of 2 water molecules which are adsorbed on a cluster of 3 oxygen vacancies (O_{vac}) on the TiO_2(001)-(3×2)
Figure S2. Electronic Energy Bands and Partial Densities of States of TiO$_2$(001)-(3x2) with 3 O$_{\text{vac}}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=5 for Ti 3$d$ states.
Figure S3. Electronic Energy Bands and Partial Densities of States of TiO$_2$(001)-(3x2) with 3 O$_{\text{vac}}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=6 for Ti 3$d$ and U=3 for O 2$p$ states.
2. Dissociation of 2 water molecules which are adsorbed on a cluster of 3 oxygen vacancies (O$_{vac}$) on the TiO$_2$ termination of PbTiO$_3$(001)-(3×2)

Figure S4. Total charge density plot of PbTiO$_3$(001)-(3×2)-TiO$_2$ terminated + 3 O$_{vac}$ + 2 H$_2$O system. Ball-and-stick illustration of the lattice structure with Pb (dark gray), Ti (light blue), O (red), and H (white).
Figure S5. Electronic Energy Bands and Partial Densities of States of PbTiO$_3$(001)-(3x2)-TiO$_2$ termination with 3 $O_{\text{vac}}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=5 for Ti 3$d$ states.
Figure S6. Electronic Energy Bands and Partial Densities of States of PbTiO$_3$(001)-(3x2)-TiO$_2$ termination with 3 O$_{\text{vac}}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=6 for Ti 3$d$ states.
Figure S7. Electronic Energy Bands and Partial Densities of States of PbTiO3(001)-(3x2)-TiO2 termination with 3 O\textsubscript{vac} and with 2 H\textsubscript{2}O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=6 for Ti 3d and U=3 for O 2p.
3. Dissociation of 2 water molecules which are adsorbed on a cluster of 2 oxygen vacancies ($O_{\text{vac}}$) on the PbO termination of PbTiO$_3$(001)-(3×2)

Figure S8. Total charge density plot of PbTiO$_3$(001)-(3×2)-PbO terminated $+ 2 O_{\text{vac}} + 2 \text{H}_2\text{O}$ system. Ball-and-stick illustration of the lattice structure with Pb (dark gray), Ti (light blue), O (red), and H (white).
Figure S9. Electronic Energy Bands and Partial Densities of States of PbTiO$_3$(001)-(3x2)-PbO termination with 2 O$_{vac}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=5 for Ti 3d states.
Figure S10. Electronic Energy Bands and Partial Densities of States of PbTiO$_3$(001)-(3x2)-PbO termination with 2 O$_{vac}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=6 for Ti 3$d$ states.
Figure S11. Electronic Energy Bands and Partial Densities of States of PbTiO$_3$(001)-(3x2)-PbO termination with 2 O$_{\text{vac}}$ and with 2 H$_2$O at two adjacent oxygen vacancy sites. Calculated using SCAN+U method with U=6 for Ti 3$d$ and U=3 for O 2$p$ states.